



Density – A contentious issue in the evaluation and determination of Resources and Reserves in coal deposits

L. Roux¹

Affiliation:

¹ Leon Roux
Retired from Exxaro's
Grootegeluk Coal Mine and
continued with the Clean Coal
Research Group at the
University of the Witwatersrand
during his research years
preparing for this paper.
Post Humous.

Correspondence to:

L. Roux

Email:

rouleo@outlook.com

Dates:

Received: 8 Mar. 2019
Revised: 6 Aug. 2020
Accepted: 24 Feb. 2021
Published: May 2021

How to cite:

Roux, L. 2021
Density – A contentious issue in
the evaluation and determination
of Resources and Reserves in
coal deposits.
Journal of the Southern African
Institute of Mining and Metallurgy,
vol. 121, no. 5, pp. 227–250.

DOI ID:

<http://dx.doi.org/10.17159/2411-9717/17386/2021>

Synopsis

The initial evaluation of a coal deposit often raises uncertainty with regard to the accuracy of the reported Resources and Reserves. Reconciliation of results from mining and beneficiation with the original raw field data highlights deficiencies in original estimations. Credible Resource and Reserve estimation forms the basis on which an entire mining enterprise is motivated, initiated, funded, and established as a commercially viable proposition. This is required for sustainable extraction purposes and to support vital downstream industries such as power generation.

Accurate determination of the density of the matrix of the material being evaluated is the key to credible values being obtained for Resources and Reserves. Losses between 15% and 20% of the Resource/Reserve can be realized if incorrect densities are applied to the tonnage derivation. Coal plies and particles have different relative densities, determined by the maceral composition, rank, and mineral and moisture content. These factors in turn contribute to the moisture, volatile matter, ash and carbon contents of a coal, which affect the overall density of the raw coal. More specifically, the relationship of ash to density and the effective matrix porosity were found to be critical in solving the greater majority of the problems in predictive calculations.

A major deficiency identified is the inability to determine effective porosity, allowing absorption of adventitious moisture and altering the mass of the core sample. Although the volume of the raw material is altered through crushing, the change in mass after controlled air-drying, used with the original geometrical volume of the raw material, provides a credible air-dry density and allows the determination of the volumetric change related to effective porosity. This parameter can be validated through the evaluation of proximate ash using the ash-adjusted algorithm and a correction for the inherent moisture applied to also give a credible relative density value for an air-dried sample.

A combination of theoretical, empirical, and reconciliatory evaluations of the available data, taken from the exploration phase through the mining process to final production, has shown that an integrated approach using the ash-adjusted density (AAD) methodology, in conjunction with other evaluative techniques, provides credible results with a considerably higher degree of accuracy than is currently possible.

Keywords

coal, deposit evaluation, Resources, Reserves, density determination, ash-adjusted density.

Introduction

The evaluation of coal deposits from exploration through Resources and Reserves classification, mining and prediction of grades, application of interpretive measures in the overall evaluation of coal deposits, the behaviour of the raw feed material in the beneficiation process, and the final mass accounting of saleable products may be enhanced through the application of the ash-adjusted density (AAD) methodology (Roux, 2012)

Many uncertainties affect budgetary and forecasting purposes and the definition and quantification of saleable reserves. This is problematic in most coal deposits, particularly those related to specialized products with very strict quality specifications in newly developing coalfields or previously unexplored regions, which could be far more variable and difficult to assess than deposits in conventionally mined areas where a wealth of data has already been accumulated over time. Basic information that has been used historically for the determination of Resources and Reserves may be instrumental in portraying misleading results relating to either under- or overestimation of Resources and Reserves, especially in relation to tonnage estimations.

The crux of the matter relates to the accuracy of the density of the material being evaluated. Density *per se* underpins all Resource and Reserve estimations as well as reconciliation after mining. An in-depth study is required of not only the methods of density determination, but including variations with regard to the geology of the deposit, specifically the composition of the coal, the composition of its solid

Density – A contentious issue in the evaluation and determination of Resources and Reserves

matrix, its rank, type, and grade, and pore fluids or gases, which all have an effect on the *in-situ* as well as air-dry or absolute density of the matrix material.

Preston and Sanders (2005) very aptly describe the situation relevant to probably one of the more important aspects at the beginning of the value chain. Density is a contentious issue. 'The relative density of coal is a fundamental physical parameter which should be well understood by geologists, who need to know the *in situ* relative density of coal for use in reserve calculations.' This, according to the authors, appears to be poorly understood and unfortunately also poorly documented, with virtually no practical definitive work having been done, apart from that of Smith (1991). Thus, the application of relative density in Reserve calculations is uncertain, or at worst incorrect. Quality Coal Consulting conducted a study for Pacific Coal (Preston and Sanders, 2005) to address this problem, with primary consideration being given to the relationships between coal density, coal porosity, and moisture. A prerequisite of any evaluation is the validation of the basic information from the original source. Uncertainty here could have far-reaching effects on the eventual evaluation of the deposit, especially with regard to its economic viability and sustainability.

In South Africa, all Coal Resources and Coal Reserves are classified according to the SAMREC Code and SANS10320:2004, which outline the standard method of reporting of Coal Resources and Coal Reserves through the application of the various technical parameters, and specifically the determination of GTIS (gross tons *in situ*), TTIS (total tons *in situ*) and MTIS (mineable tons *in situ*). Venmyn Deloitte found considerable inconsistency in the reporting of Coal Resources in the minerals industry, and particularly among South Africans and Australians. Some companies used GTIS, some used TTIS, and others used MTIS, with some reporting on all of these values in the interest of clarity. Note that the evaluation done here is based on information from the only currently operating mine in the Waterberg Coalfield in South Africa.

The JORC Code and the Australian Guideline for Estimating and Reporting are not as prescriptive, although the Guideline states that, 'Coal resources should be estimated and reported for individual seams or seam groupings within a deposit. They should also be subdivided and reported on the basis of key variables, such as thickness, depth range, strip ratio, coal quality parameters, geographic constraints and geological or technical considerations. The key variables and assumptions for each deposit should be clearly stated in order to ensure clarity and transparency of the report.' However, in a South African scenario, the use of different reporting standards for Coal Resources was found to be particularly problematic.

One particular scenario raising concern with regard to Coal Resource reporting highlighted by Venmyn Deloitte refers to the Waterberg Coalfield, where multiple seam deposits with intercalated shales occur in the Volksrust Formation. The multiple seams are delineated into sedimentary depositional zones, and sampling of these zones in some cases does not separate the coal from the interlaminated shale portions. The zones are modelled and the tonnages calculated, and Resource statements have quoted the tonnages pertaining to the whole zone rather than only the coal portion, which according to Venmyn can be misleading.

Venmyn Deloitte noted that the coal industry in South Africa is attempting to standardize one method of reporting. This has

led to a re-assessment and re-writing of the SANS Code, which is currently underway. Revisions proposed have been used in this paper and the most critical initial values have been singled out for evaluation.

Considering the SAMREC Code and proposed revisions of SANS 10320: 2004, *Mineable Tonnes In Situ Coal Resource* refers to the tonnage and coal quality, contained in the coal seam, or section of the coal seam proposed to be mined, at the theoretical mining height, adjusted by *geological loss factors* and specific mining methods after the relevant minimum and maximum mineable thickness cut-offs and relevant coal quality cut-off parameters have been applied. For Public Reporting purposes all Coal Resource tonnages and coal quality must be reported *as a Mineable Tonnes in situ Coal Resource (MTIS basis)*, with associated yield, coal quality and moisture content.

Coal Reserve reporting refers to, the Coal Reserve that is the economically mineable part of a Measured and / or Indicated Coal Resource, which includes diluting and contaminating materials and allowances for losses, which may occur when the material is mined or processed and is defined by studies at Pre-feasibility or Feasibility level, as appropriate, that include application of Modifying Factors and such studies which demonstrate that, at the time of reporting, extraction could reasonably be justified.

Key issues for the derivation of primary tonnage estimates are:

1. The *in situ density* of the coal adjusted from the laboratory determined relative density taking analyzed moisture content related to the *in situ* bed moisture content into account.
2. *Geological loss factors* applied to resource tonnages.
3. Theoretical mining height of the coal seam, or the optimal selected part of the coal seam that is expected to be mined, based on a geological assessment
4. The Resource that will be upgraded by washing in a coal processing plant, quantified by washed coal quality data for quality points of observation
5. The theoretical product yield being the laboratory estimate of the yield of the target product at a specific coal quality, or at a specific cut-point density, on an undiluted and uncontaminated basis.

Another point that could be added refers to the type of coal deposit.

6. A thick inter-bedded seam deposit or a multiple seam deposit.

The credibility of Coal Resource and Reserve estimations currently and conventionally obtained is questionable.

This relates to actual mined data being irreconcilable with the original raw data obtained from basic field evaluations during exploration. This is specifically applicable when *in-situ* raw density obtained through the application of the Archimedes principle in the determination of SG is used for tonnage estimations in geological modelling, mine planning, scheduling, budgeting, and production.

Problems experienced in correct tonnage estimations are largely due to the inability of the processes applied to establish an appropriate and verifiable reconciliation of material from Resource through the value chain of extraction, beneficiation, to production, including product tonnage prediction. Pre-determined predicted Resources and Reserves are essential for planning and

Density – A contentious issue in the evaluation and determination of Resources and Reserves

scheduling of appropriate feed material to be supplied from the mine to the beneficiation plant and ultimately for the production of specified saleable products. This problem is further exacerbated by limitations with regard to accurate physical measurements that are needed to validate the results. Therefore, measurement, monitoring, and correct estimation are key issues in question.

Review

An assessment of tonnages extracted and compared to the original planned and budgeted figures, as well as attempts at reconciling the final data with the original basic data used for the determination of Resources and Reserves, has highlighted critical deficiencies in the entire process. These deficiencies are related to both the initial evaluation methods and the mining process (Roux, 2010).

To begin the assessment, the suggested addition of the type of coal deposit will be reviewed before the issues highlighted in the SANS proposed changes.

The type of coal deposit

The Volksrust Formation, classified as a thick interbedded seam deposit and which forms the upper part of the coal deposit, comprises intercalated shale and bright coal layers with an average thickness of about 60 m (Figure 1). It displays such a well-developed repetition of coal-shale assemblages that it can be divided into seven major sedimentary cycles or zones. Smaller sub-cycles ('samples') are contained within these zones; these were sampled individually during exploration of the deposit. The terms 'zone' and 'sample' are used at Grooteegeluk instead of 'seam' and 'ply' due to the site-specific intercalated nature of the coal and shale.

The Volksrust Formation zones typically start with bright coal at the base, with the ratio of coal to shale decreasing from the base of each zone upwards. The Basal Zone is the exception because the coal is more evenly distributed throughout this zone. The shales of the Volksrust Formation show an increase in carbon content with depth and range from a massive bluish-grey mudstone at the top to carbonaceous shales towards the Basal Zone.

Although the thickness and coal quality of the Volksrust Formation zones are reasonably constant across the coalfield, a large variation in the yield of semi-soft coking coal occurs vertically in the coal succession.

The mineralogy of the Volksrust Formation is dominated by kaolinite, quartz, and minor amounts of apatite in the lower portion while the upper portion is dominated by quartz, kaolinite, and minor amounts of montmorillonite, illite, and microcline. Calcite lenses occur predominantly in the upper half of the Volksrust Formation and have been interpreted as being syndepositional. Diagenetic globular pyrite and spherulitic siderite occur in the coals and organic-rich mudstones. The mineralogy of the mudstones and trace element concentrations suggest deposition in fresh water rather than marine waters. (Faure *et al.*, 2002).

At Grooteegeluk the zones were subdivided into sub-cycles (samples). The individual samples from the Volksrust Formation were further subdivided into a coal and shale component for stringers thicker than 1 cm. Stringers of less than 1 cm thickness were included in the overriding lithology, *i.e.* coal stringers in shale less than 1 cm were retained in the shale samples, while the same applies to shale stringers in coal samples. The coal and

the shale components were analysed separately to enhance grade control functionality. The reasoning behind this was that if part of a recognized sample was left in the floor, or conversely mined out previously, this could be taken into account when compiling the mined vertical sequence and an adjustment pertinent to the actual material could be made.

The analytical results for the individual components were then composited to obtain values for the entire sample, including both the shale and coal components. Unfortunately, a Resource value for only the coal component (as suggested by Venmyn Deloitte) was not feasible due to the intercalated nature of the coal and shale components. The Resource would have to be beneficiated in order to extract economically viable coal, thus the shale component of these sub-cycles (samples) needs to be recognized as part of the Resource.

The Vryheid Formation (approximately 55 m thick) forms the lower part of the coal deposit and comprises carbonaceous shale and sandstone with interbedded dull coal seams varying in thickness from 1.5 m to 9 m (Figure 2). The Vryheid Formation is classed as a 'Multiple Seam Deposit Type' according to the SAMREC Code. There are five coal seams or zones in the Vryheid Formation, all of which are composed predominantly of dull coal with some bright coal developed at the base of zones 2, 3, and 4. Due to lateral facies changes and changes in the depositional environment, these zones are characterized by a large variation in thickness and quality.

Zone 3 is the best-developed dull coal zone within the mine lease area, reaching a maximum thickness of 8.9 m. The basal portion of this zone yields a small fraction that has semi-soft coking coal properties.

Zone 2 is, on average, 4 m thick and reaches a maximum thickness of 6 m in the mine lease area. The basal portion of this zone also yields a fraction that has semi-soft coking coal properties. This zone is the most constant of all the Vryheid

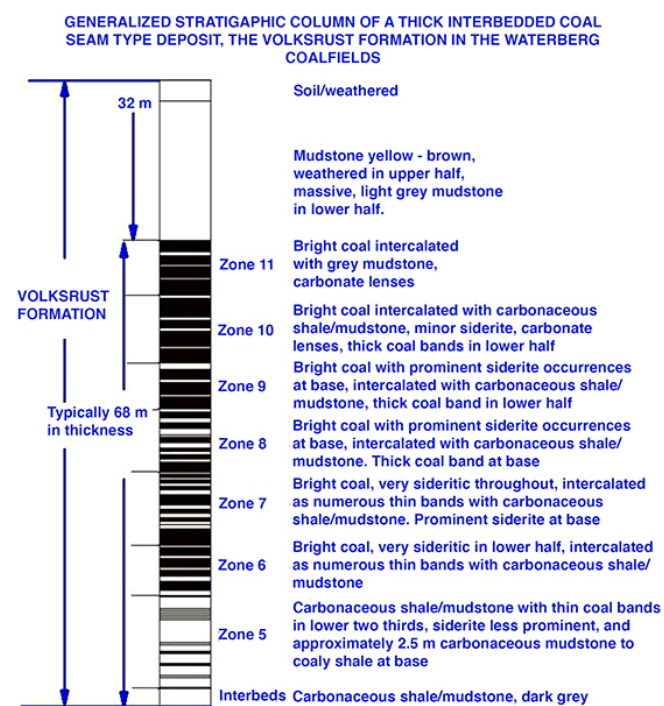


Figure 1—Generalized stratigraphic column of thick interbedded coal seam type deposit of the Volksrust Formation at Grooteegeluk Coal Mine, indicating zonal delineation

Density – A contentious issue in the evaluation and determination of Resources and Reserves

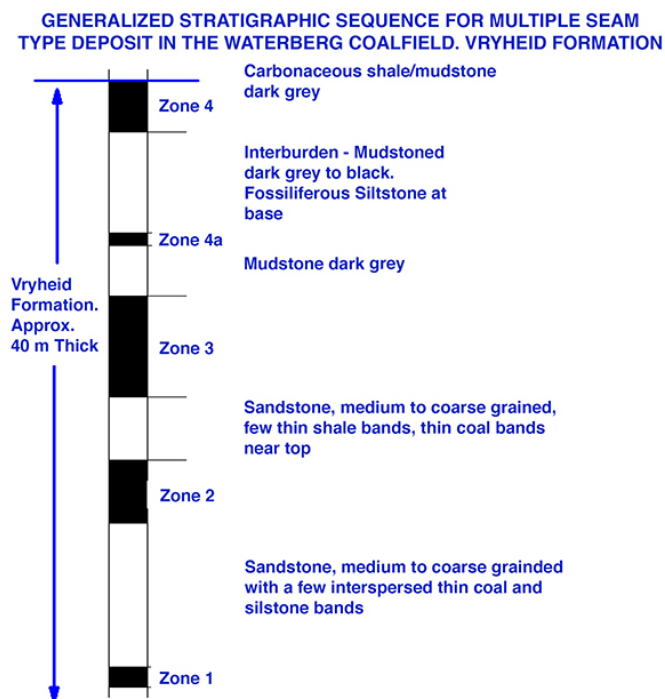


Figure 2—Cyclic sedimentary subdivision of coal sequence for the Vryheid Formation

Formation coal zones across the entire Waterberg Coalfield regarding thickness.

Zone 1, the basal Vryheid coal zone, has an average thickness of 1.5 m, but varies quite rapidly being the lowermost coal layer in the sequence.

The distinct differentiation between the Volksrust Formation and the Vryheid Formation illustrates two different depositional environments, the Volksrust Formation being representative of an autochthonous deposit, while the Vryheid Formation is typically an allochthonous deposit.

The Vryheid formation is defined as a multiple seam deposit although also subdivided into sub-cycles for the individual seams. Each seam is treated as a single entity, coal only, therefore the Resources representing the seam are relevant to coal only.

In-situ density

Before one can consider determining the *in-situ* density of the coal an in-depth understanding of the matrix within the volume of the coal sample is required. Which properties of the matrix would have the greatest influence on the determined density of the coal? Would it be the volume occupied by the matrix, its mineral content, its moisture content, or its void content (porosity), also taking its permeability into account? The most basic definition of density refers to the mass per unit volume of the material being assessed.

$$\text{Density} = \text{Mass/Volume}$$

The volumetric component is the most complex property in the determination of the density of the material being evaluated.

The typical definition of volume in most dictionaries is given vaguely as 'the space occupied by an object'. McGraw-Hill's Dictionary of Scientific and Technical Terms (1984) does not say much more, their definition merely relates the object to three-dimensional space: 'A measure of the size of a body or definite region in three dimensional space ...' In order to appreciate

the various conditions under which volume is defined, particle technology's lexicon used for these definitions can be found in the British Standards Institute (BSI,1991) and the American Society for Testing and Materials (ASTM,1994) documents. Here the 'volume' of a material is described as the summation of several rigorously defined elemental volumes.

A cylindrical length of rock core can be used as an example of an object that contains all types of elemental volumes and differences in material volume according to the measurement technique, measurement method, and conditions under which the measurements are performed.

The rock core, obviously, is solid material with a volume that can be calculated after measuring its length and its diameter, from which its cross-section can be determined. However, it also contains surface irregularities, small fractures, fissures, and pores that both communicate with the surface and pores that are isolated within the structure. Voids that connect to the surface are referred to as open pores while interior voids inaccessible from the surface are referred to as closed pores. Surface irregularities compose another type of void volume. For example, assume the bulk volume of the core is determined from linear measurements of its length and cross-section. The value of volume determined in this way is limited in accuracy because the surfaces are not perfect. If a perfect plane were to be laid on one of the surfaces of the core, there would be many voids sandwiched between the two surfaces (Figure 3).

For lack of a standard definition, this can be referred to as 'external void volume' and will refer to the void volume between a solid surface and that of a closely fitting envelope surrounding the object. It does not include pores that penetrate the interior of the particle. The meaning of the term is admittedly vague, but this volume can be determined or estimated under certain analytical conditions and can provide an indication of surface rugosity. When a solid material is in granular or powdered form, the bulk contains another type of void: interparticle space. The total volume of interparticle voids depends on the size and shape of the individual particles, their sorting, and packing. (Webb, 2001)

The complexity of the term volume is highlighted by the following definitions:

- **Absolute powder volume:** (also called absolute volume): The volume of the solid matter after exclusion of all the spaces (pores and voids) (BSI).

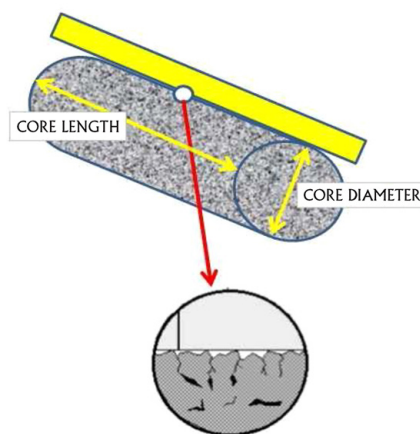


Figure 3—A straight edge placed along the outside edge of the length of core demonstrating the concept of 'external volume', the volume contained by virtue of surface irregularities (Micromeritics Instrument Corp., 2000)

Density – A contentious issue in the evaluation and determination of Resources and Reserves

- **Apparent particle volume:** The total volume of the particle, excluding open pores, but including closed pores (BSI).
- **Apparent powder volume:** The total volume of solid matter, open pores, and closed pores and interstices (BSI).
- **Bulk volume:** The volumes of the solids in each piece, the voids within the pieces, and the voids among the pieces of the particular collection (implied by ASTM D3766).
- **Envelope volume:** The external volume of a particle, powder, or monolith such as would be obtained by tightly shrinking a film to contain it (BSI). The sum of the volumes of the solid in each piece and the voids within each piece that is, within close-fitting imaginary envelopes completely surrounding each piece (implied by ASTM D3766).
- **Geometric volume:** The volumes of a material calculated from measurements of its physical dimensions.
- **Skeletal volume:** The sum of the volumes of the solid material and closed (or blind) pores within the pieces (implied by ASTM D3766).
- **True volume:** Volume excluding open and closed pores (implied by BSI).
- **Void:** Space between particles in a bed (BSI).

If particle characteristics as shown in Figure 4 are re-evaluated, the envelope volume (Figure 5) can be considered as being representative of a cross-section of the core sample retrieved from the borehole. It represents the geometric volume derived from the product of the cross-section of the core and its length, not taking rugosity shown in the figure into account and assuming that the core is an absolute solid.

Density derived from this would then simply be determined by the mass of the core divided by its bulk volume. No free moisture content is known since the core was not impeccably preserved on recovery and no moisture determination was done.

In the next case, reflecting probable skeletal volume, the core is subjected to Archimedes principle for SG determination and assuming saturation of the core, its mass in air divided by the difference between the mass in air and the mass in water gives a specific gravity for the entire sample, which is greater than the original density determined on the core as received. This is the result of water ingress during the procedure (Figure 6).

The core dispatched to an accredited laboratory is weighed on receipt, crushed, and screened to $-13\text{ mm} +0.5\text{ mm}$, air-dried under controlled conditions, and re-weighed before float/sink analyses are done. The air-dry mass is substantially less than the recovery mass; using this mass and the original envelope volume of the core results in a density substantially lower than the first two values obtained. This, however, is not representative of the true air-dry mass of the sample because the mass of the -0.5 mm fraction after screening is not reported or shown in the geological database. This -0.5 mm material is, however, used for a raw proximate analysis of the sample. The density value obtained cannot be deemed representative of the air-dry density and as such cannot be used to derive an accurate estimate of air-dry skeletal volume (Figure 7) of the matrix.

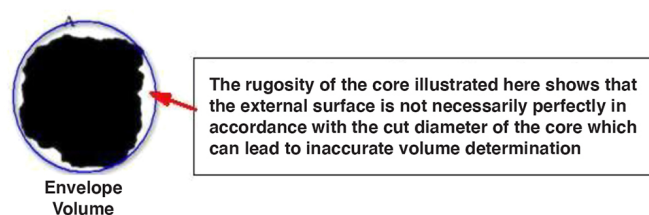


Figure 5—Envelope volume

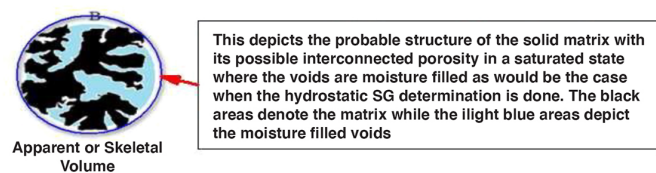


Figure 6—Apparent moisture-saturated skeletal volume

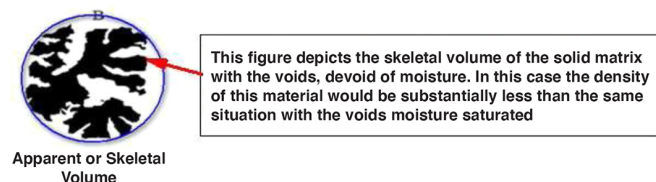


Figure 7—Air-dry skeletal volume

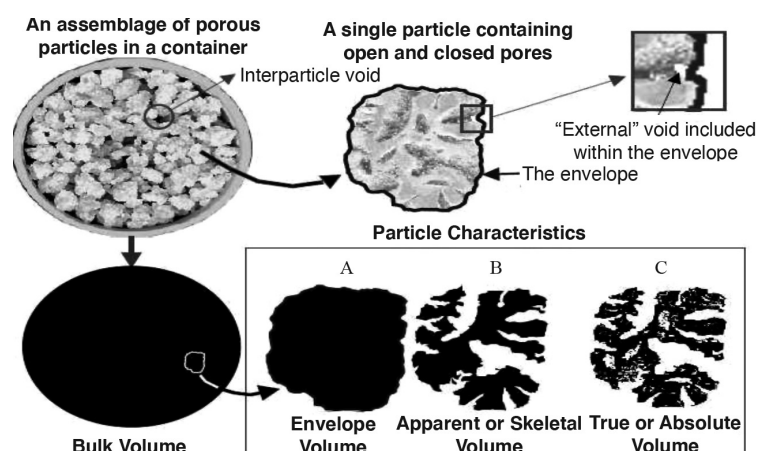


Figure 4—Illustrations of various volume types. At the top left is a container of individual particles illustrating the characteristics of bulk volume in which interparticle and 'external' voids are included, at the top right is a single porous particle from the bulk. The particle cross-section is shown surrounded by an enveloping band. In the illustrations at the bottom, black areas are analogous to volume. The three illustrations at the right represent the particle. A is the volume within the envelope, B is the same volume minus the 'external' volume and volume of open pores, and C is the volume within the envelope minus both open and closed pores (Webb, 2001)

Density – A contentious issue in the evaluation and determination of Resources and Reserves

In order to determine the solid matrix percentage, the core needs to be absolutely air dry, its mass determined, and then submerged in water for the Archimedes determination of SG. If the Archimedes SG determination is conducted properly, allowing for complete saturation so that no air bubbles are observed during the submerged phase, the SG can be used to determine the volume capable of supporting that density for the air-dried mass of the core. This in turn can be subtracted from the original volume and the result expressed as a percentage of the original volume representing voids in the matrix. This percentage subtracted from 100% would be representative of the solid matrix of the core.

The last scenario, shown in Figure 8, depicts the absolute volume; here both interconnected porosity and closed porosity are shown. The closed porosity may contain gas, air, or moisture. The moisture may be representative of the inherent moisture, which can be released only during combustion. If the absolute dry density can be determined and the mineral volatile content, including inherent moisture, is known or determined, the air-dry density of the sample can be determined.

Considering the requirements for Coal Resource tonnage reporting and the stipulation that these tonnages are reported as 'mineable tonnes *in situ*' raises another problem if the *in-situ* moisture content of the coal beds is unknown. Groundwater levels, porosity, and permeability would greatly influence the *in-situ* density of the material being assessed. Consider two scenarios sketched in Figure 9, the first illustrating an exploration borehole intersecting a coal sequence under the groundwater table, the probability of the core retaining the moisture when it is recovered is relatively good. This core should, however, be immediately sealed to prevent moisture loss, sent to the laboratory and the moisture content determined. This moisture content would represent the *in-situ* moisture of the core. In the second example, in a purported dry borehole, the core may still contain some moisture, relating initially to interstitially trapped water and secondly to structural or inherent moisture. These values should also be ascertained since they will influence the overall apparent relative density of the material.

A third scenario to consider, sketched in Figure 10, is an exploration borehole that may have been drilled several years



This figure depicts both the interconnected voids as well as voids within the matrix that are not interconnected and may contain trapped moisture or air/gas. The black skeletal structure represents the solid matrix and as such, less than the previous figure. This material would represent the absolute volume of the matrix material

Figure 8—Absolute volume

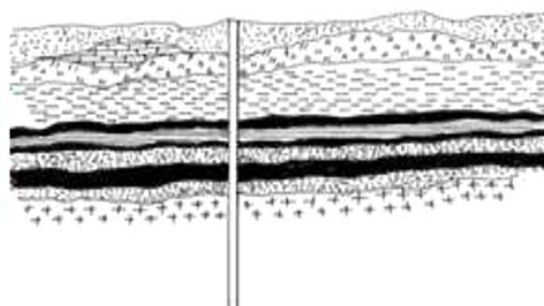
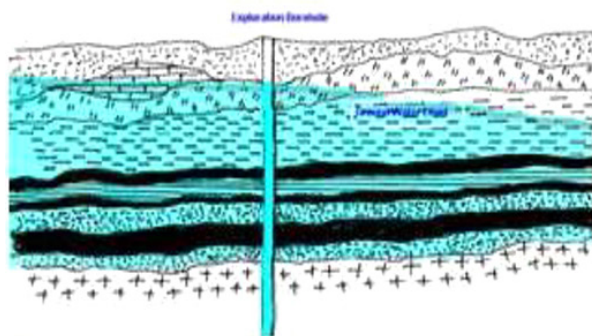


Figure 9—(Left) Coal measures below groundwater level, (right) coal measures essentially dry – no groundwater influence

earlier, prior to any mining activities, but is now in a position where an opencast mining operation has advanced closer to the specific exploration borehole from which the original determinations were done. Groundwater, having drained from this area into the mine's sump over the years, is now at a level below some of the coal seams and the mining benches have been exposed to natural atmospheric and climatic conditions for several years, thus rendering them effectively dry.

Information with regard to *in-situ* densities determined during the exploration phase, used for mineable tons *in situ* determinations, is no longer valid since the moisture content in the subsurface environment has changed over time.

Consider what the *in-situ* moisture content of this material would be. Assuming this is the same borehole shown in the first scenario (Figure 9, left), the moisture content in the upper benches may be the same as for the borehole drilled through a dry area, similar to the one shown in Figure 9, right. Surely it is no longer feasible to use the values initially obtained for an apparent relative density, especially if they were derived using the Archimedes principle method?

The most logical value to use would be representative of the air-dry relative density, which at least partially conforms to the material being mined. This value would allow more credible Resource and Reserve tonnage estimation and an improved planned volume of material to be extracted in order to satisfy budgetary predictions. Planned mining extraction should rather be based on volumes to be extracted in order to produce the required tonnages of matrix material.

Density and porosity

Traditionally, the basic method of determining the relative density of an assumed solid, such as coal, is to weigh it in air, then immerse it in water and weigh it again, the relative density being equal to the ratio of the weight in air to the loss of weight in water.

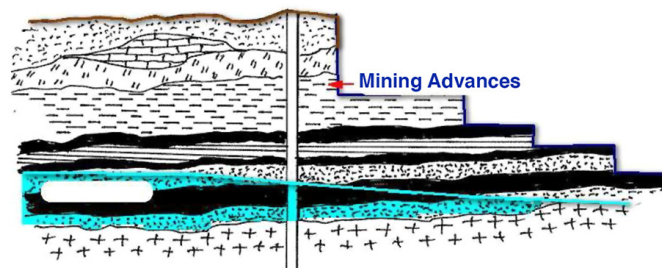


Figure 10—Opencast mining approaches the exploration borehole, illustrating the effect of the drainage of groundwater over time

Density – A contentious issue in the evaluation and determination of Resources and Reserves

Analyses done by the University of Illinois as early as 1916 on relative density (at that time referred to as specific gravity) under varying conditions of moisture content add a whole new perspective to density determinations (Nebal, 1916).

The American Society for Testing and Materials book of standard definitions lists no less than 40 definitions for density based on mass per unit volume. The British Standards Institute reduces this to 14. The determination of the mass of an object is relatively straightforward; the determination of the volume, however, is complex. The volume of a solid object, whether it is a single piece or a mass of finely divided powder, is a concept that cannot be ascribed to a single, neat definition.

A more specific definition of relative density (RD)

At a temperature of 5°C the density of water is 1.0 g/cm³, thus the relative density of a material is its density relative to the density of water at 5°C. This property is a ratio, thus dimensionless, and is numerically equivalent to the density of the material. All relative density determinations require the mass and the volume of the material to be measured. The mass determination is simple; the volume determination however, as discussed earlier, both in regard to measurement and understanding in heterogeneous materials such as coal, is complex. This relates primarily to the porosity of coal and the variable degree to which different methods cope with this aspect of the determination. Since coal is porous, most of the contained moisture is held physically in its pores. The pores may be interconnected or isolated. Interconnected pores contribute to permeability thus, when coal is dried, its permeability allows some of the moisture to leave the pores, which become filled with air. If the dry coal is placed in water, the air in the pores is displaced by the water, and the coal becomes saturated. Under such circumstances the length of time that the coal is immersed before it is weighed affects the value obtained for the relative density.

True (or absolute) relative density should only be used to describe the relative density of a volume of pore-free coal, which by implication means that whichever method is used in determining the volume of the sample, the medium used must occupy all the pores, which in practice is very difficult. Helium, being the smallest atom, has the best probability of penetrating the greatest number of pores, thus the helium density method is the recognized method for determining this parameter. The availability of consistently reliable true or absolute relative density values for coal would make the estimation of *in-situ* relative density a straightforward process.

Apparent (or coal particle) relative density describes the relative density of lump coal which may contain pores, fissures, and moisture, the persistence of which in the actual sample may be variable, tending to give unreliable results when density is determined by the Archimedes method. A more precise determination can be obtained by use of the mercury density method, but similar to the helium method, the equipment required is not always available.

In-situ relative density

In-situ relative density refers to the relative density of the coal in the ground. The coal under confining pressure contains pores and fissures filled with water and dissolved gases. The relative density measurement of the coal *in situ* is the value that is used for the estimation of Coal Resources. This value may be calculated from the coal thickness (*in situ*), the core diameter, and the mass of impeccably preserved core lengths. The Australian Standard

method of determining coal density is most commonly used, and although the method is cheap and easy to apply, the state of the sample when tested does not simulate the *in-situ* condition of the coal because the sample is ground to –212 µm, removing fissures and some pores. It is also air-dried, retaining its inherent moisture. The moisture thus retained is representative of the inherent moisture of the coal sample as determined by proximate analysis on the same sample.

The method involves measuring the liquid displacement, in either a density bottle or a volumetric flask, thus determining the volume of the ground coal sample; this is then related to the original weighed mass. The major problem with the method is the inability of the liquid to occupy all pores within the coal and thus displace all air and water. The result gives neither absolute relative density nor an *in-situ* relative density, although it is probably closer to the absolute relative density. Under rigorously controlled conditions, the standard density bottle method may give results closely approximating the true or absolute relative density for coal expressed on the air-dry basis.

This standard method does not replicate the conditions required for determination of *in-situ* relative density since the values obtained are tested on an air-dry basis, whereas the resources of coal *in situ* are not; the use of standard relative density in Resource and Reserve calculations is thought to result in an overestimation of Reserves. In order to convert the standard relative density to an *in-situ* relative density, the sample needs to be reconstructed to simulate original conditions, especially with relevance to the original volume, restoring the pores and fissures destroyed in the grinding process. The reduction in volume of the sample has a greater effect on the relative density than the loss of mass held in that volume.

If the voids are restored to their original state and refilled with water, both the volume and mass will increase. The volume, however, will increase at a rate higher than the mass and thus the sample density will decrease, trending towards unity, the relative density of water. The most critical information required here relates to the *in-situ* moisture content of the sample, since this would be essential for the calculation of densities, Reserves, coal handling mass calculations, and the estimation of product coal total moisture. To assess the *in-situ* moisture content of the samples, cores should be promptly bagged and sealed so that the total moisture retained can be determined by a laboratory.

Research at the University of Illinois in 1916 on the effects of coal porosity illustrated the fact that the voids were air-filled as a result of being air-dried, the air being expelled when the sample was submerged in water for the density determination. This indicated the inherent problems that could be expected in determining the relative density of coal. It also indicated the differences in the specific gravity values obtained for purported fresh coal as opposed to the 'true' specific gravity of air-dried coal and the moisture contents of these coals. Several experiments were conducted to determine the effect on specific gravity of the expulsion of air through the replacement of water in the voids in an air-dried coal, as well as the time required for the expulsion of the air from interconnected voids. One of the interesting experiments in this range compared the specific gravity of fresh coal and that of the same dry coal. A range of samples were allowed to dry in the laboratory under constant temperature for 60 days. The specific gravity of the fresh coal averaged 1.28 g/cm³ while that of the air-dried coals was 1.19 g/cm³. The same samples were then subjected to boiling water in order

Density – A contentious issue in the evaluation and determination of Resources and Reserves

to dispel air and the voids, now filled with water, raised the SG to 1.31 g/cm³. From this it was deduced that the moisture loss of the fresh coal was dependent on the original moisture content of the coal, the porosity of the coal, the humidity in the air to which the coal was exposed, and the final loss dependent on the period of time that the coal was exposed to air. Subsequent experiments were then done to ascertain the density of coal samples from an air-dry condition to probable full saturation, and the concomitant changes in apparent density over time. It is interesting to note that the greatest change took place within the first two hours, as shown in Figure 11.

The experiment was repeated with the values being determined over shorter time periods to assess the rate of change within the first 2 hours. This is shown in Figure 12. Here again the greater part of the change was noted within the first hour of immersion, the specific gravity increasing from 1.16 g/cm³ to approximately 1.30 g/cm³, and eventually to 1.32 g/cm³ after two hours.

This early experimental work highlights the possible error with regard to so-called relative density and the effect on the relative density as a result of, the porosity of the medium and whether the pores are air- or water-filled. The effective porosity or moisture-holding capacity would have to be taken into account when considering which value of 'relative density' should be used in Resource and Reserve tonnage determination.

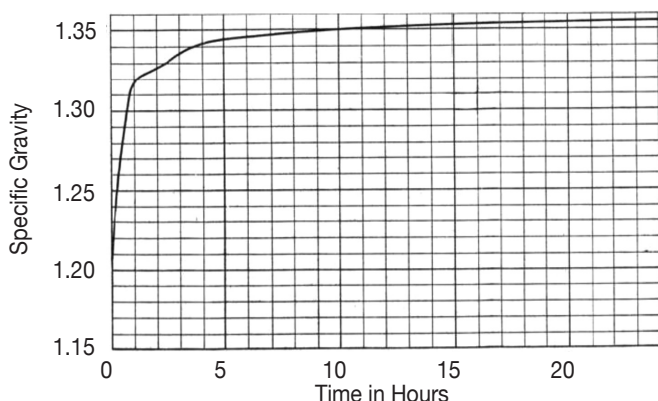


Figure 11 – Graphical representation of the increase in specific gravity over 24 hours in a coal sample submerged in water at room temperature (Nebal, 1916)

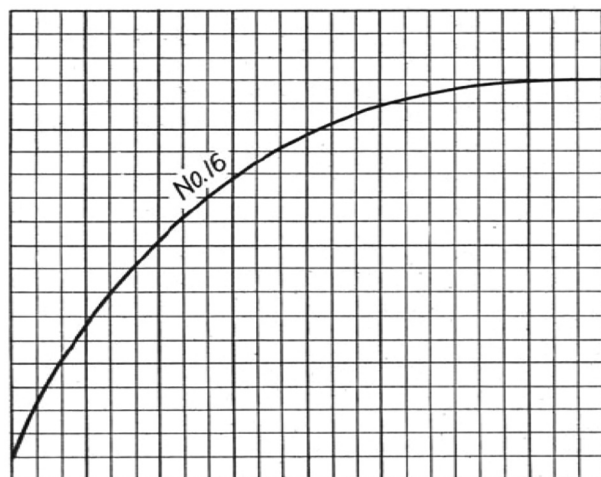


Figure 12 – The change in specific gravity of coal samples immersed in water at room temperature (Nebal, 1916)

Considering values obtained in the field, such as relative density determined by the Archimedes principle, and the availability of appropriate information, it is extremely difficult to assess the relevant *in-situ* density of the coal from data obtained at the exploration site. These initial values, however, can be partially validated when the laboratory results are received.

Literature studies and personal communication with experts in the field (Pinheiro, pers. comm.) has revealed the most common methods of determining *in-situ* relative density are by the Archimedes principle and by pycnometry through the application of the Australian Standard method (AS1038.21 Item 4). The value obtained from the Australian Standard method should not be used for Reserve calculations since the values obtained are on an air-dry basis and coal Resource/Reserve calculations are not – they are based on *in-situ* values. The sample used for this determination, after preparation, is no longer representative of its original state with regard to volume and moisture content and can therefore result in an overstatement of Reserves (Preston and Sanders, 2005). Such values can be compensated to reflect the probable *in-situ* density by applying a change of basis equation converting coal relative density from one moisture basis to another, provided that the appropriate inputs with regard to moisture content are known.

The equation used for this is:

$$RD_2 = RD_1 \times (100 - M_1) / (100 + (RD_1 \times (M_2 - M_1) - M_2))$$

where

RD_1 = old RD, which is the RD determined *via* the density bottle

M_1 = Old moisture, which is moisture content determined from the original core sample as sealed and preserved in the field on extraction from the core barrel

RD_2 = new RD

M_2 = new moisture (which is moisture retained in the pulverized sample, probably representative of the inherent moisture).

This change of basis equation will enable the relative density of coal to be converted from one basis to another provided that the information used is reliable. If no information relating to the core's adventitious moisture content in the field is available, this method cannot be used.

Example:

RD from density bottle 1.93 g/cm³

Moisture content of core sample 20%

Inherent moisture from proximate analysis 2% $RD_2 = RD_1 \times$

$$(100 - M_1) / (100 + (RD_1 \times (M_2 - M_1) - M_2))$$

$$= 1.93 \times (100 - 20) / (100 + (1.93 \times (2 - 20) - 2))$$

$$= 154.4 / 81.93$$

$$= 1.88 \text{ g/cm}^3 \text{ relative } in-situ \text{ RD}$$

A different approach to the estimation of *in-situ* relative density was developed by Peabody Energy (Robeck and Huo, 2015). The mineral matter content is used with relative to estimate pure coal and mineral densities for given data-sets on a dry basis. A hyperbolic regression is then used with known *in-situ* moisture values to predict *in-situ* relative density for all raw samples.

Robeck and Huo's approach was to provide a solution for the contentious problem related to Resource and Reserve tonnage estimations through a fully deterministic RD vs. ash relationship. Their approach determining mineral matter content

Density – A contentious issue in the evaluation and determination of Resources and Reserves

was applied because ash, although representing the indestructible mineral matter, is considered a combustion product and thus not representative of the original mineral matter content. The reason for this being that mineral volatiles such as H₂O of hydration, CO₂, SO₂, salts (*e.g.*, Cl), carbonates, and sulphides are lost during combustion (Ward, 1984) and the remaining solid residue (ash) is less than the original mineral matter (Figure 13).

Complications due to (a) mineral composition, (b) coal maceral distribution, and (c) the presence of water- and air-filled pores detract from the simplistic two-phase mixture of coal and rock. Primary and secondary mineral composition may vary widely, and coal maceral content is determined by a number of factors, including rank, vegetation type, and environment of deposition (Renton, 1982).

Densities and mineral matter ratio values are shown for a few of the most common minerals in Table I. The ratio (*r*) is directly related to the percentage mass loss. This relates to the mineral volatiles percentage lost. Individual mineral densities vary and most distributions average between 2.5 and 2.8 g/cm³. The ratio can range from 1 to almost 2 depending on the mineral constituents. Similarly, the density of coal macerals can range from 1.03 to 1.70 g/cm³.

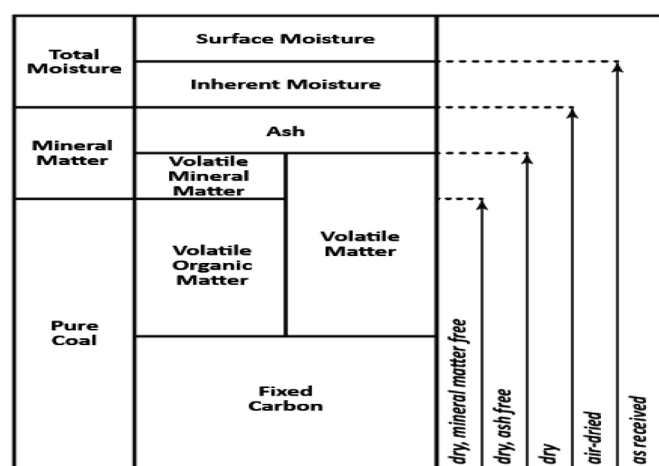


Figure 13— Relationship between the various constituents of coal and reporting bases (Ward, 1984)

Although coal density is a function of rank, increasing with degree of lithification (Smith, 1991; Sanders, 2003), maceral composition contributes to the variability of densities within the same rank. The influence of rank is attributed to changes that occur as rank increases and volatile elements (H, N, and O) are lost.

Several different models, formulations, and methods applied by various authors were evaluated by Robeck and Huo and used in the formulation of their proposed new approach correlating density to mineral matter, which would improve their predictions. The authors do, however, recognize the influence of unsaturated *in-situ* porosity and acknowledge that it has not been addressed in this method because void porosity is a volumetric percentage while the relative concentrations of coal, mineral matter, and moisture are mass weighted percentages. They claim that the amount of air-filled porosity (free gas) is small in high-rank coals and can safely be ignored in saturated coal seams. This may be true for high ranking coals, but lower ranking coals have greater effective porosity and moisture holding capacity.

Unless sampled core is impeccably preserved (sealed) on recovery so that the true moisture saturation can be determined and related to its *in-situ* state, the percentage of saturation and voids play a major role in varying determined densities for the samples. The volumetric component therefore makes a far greater contribution than mineral volatiles lost upon combustion. The authors also admit that the single greatest source of error in density estimations is the choice of *in-situ* moisture values.

Empirical formulae derived by Fletcher and Saunders (2003) based on a range of black coals (and not necessarily applicable to all basins or coal types) may have found applicability in both Australia and North America. No moisture holding capacity or equilibrium moisture data was available for their work. Their study attempted to use an empirical multivariate equation developed by Meyers *et al.* (2004). This equation proved unsuccessful so the authors used an assumed constant moisture value for coal and mineral matter that was consistent with earlier analytical work and JORC reports.

Porosity

Coal moisture content plays an integral part in contributing to

Table I

Mineral matter densities (ρ_m) and ratios (*r*) for common minerals in coal (Ryan, 1990; Vassilev *et al.*, 2010)

Mineral	Chemical composition	Abundance (%)	ρ_m (g/cm ³)	<i>r</i>	Mass loss (%)
Quartz	SiO ₂	11–56	2.65	1.00	0
Kaolinite	Al ₂ Si ₂ O ₅ (OH) ₄	14–42	2.16–2.68	1.16	14.0
Illite	KAl ₃ (AlSi ₃ O ₁₀)(OH) ₂	3–13	2.6–2.9	1.05	4.5
Montmorillonite (smectite)	($\frac{1}{2}$ Ca,Na) _{0.7} (Al,Mg,Fe) ₄ [(Si,Al) ₄ O ₁₀](OH) ₂ ·nH ₂ O	0–4	1.7–2.0	1.05	5.0
Chlorite	(Mg,Al,Fe) ₁₂ [(Si,Al) ₈ O ₂₀](OH) ₁₆	2–6	2.6–3.3	1.26	20.4
Pyrite/marcasite	FeS ₂	0.5–12	4.88–5.01	1.50	33
Calcite	CaCO ₃	1–22	2.71	1.79	44
Siderite	FeCO ₃	0–2	3.96	1.61	38
Ankerite	Ca(Mg,Fe,Mn)(CO ₃) ₂	0–3	3.05	1.79*	44
Dolomite	CaMg(CO ₃) ₂	0–6	2.84	1.91	48
Gypsum	CaSO ₄ ·2H ₂ O	0–13	2.31	1.26	20.9
Plagio-clase	NaAlSi ₃ O ₈ - CaAl ₂ Si ₂ O ₈	1–11	2.62–2.76	1.00	0
K-feldspar	KAlSi ₃ O ₈	0.5–5	2.55–2.63	1.00	0

* Assumes an average ankerite composition of 54% Ca, 24% Mg, 20% Fe, and 2% Mn

Density – A contentious issue in the evaluation and determination of Resources and Reserves

changes in relative density. Porosity *per se* provides the capacity for moisture or gas storage and is also an integral part in the overall structural composition of the materials matrix, and depending on the nature of the fluid or gas that may be contained within the pores will have an effect on the density of the material. Porosity by definition in the geological sense is the volume of the non-solid portion of the rock filled with fluids or gases, divided by the total volume of the rock, and is defined by the ratio (Anderson, 1975).

$$\phi = \frac{V_v}{V_T}$$

where V_v is the volume of void space (such as fluids) and V_T is the total or bulk volume of material, including the solid and void components. Porosity is a fraction between 0 and 1, typically ranging from less than 0.01 for solid granite to more than 0.5 for peat and clay. It may also be represented in percentage terms.

The highest porosity normally anticipated in rocks is 47.6% (Crain, 2010). A more probable porosity is in the mid-twenties range. The normal range of porosities in granular systems is 5% to 35%. In general, porosities tend to be lower in deeper and older rocks, due primarily to overburden stresses on the rock (compaction) and cementation.

Porosity in coal can be a combination of both primary and secondary porosity, the latter referring to an enhancement of overall porosity as a result of chemical leaching of minerals or the development of fractures associated with stress in the system. This can replace the primary porosity or coexist with it. Porosity can be further subdivided into effective porosity (interconnected porosity), referring to the fraction of the total volume in which fluid flow can effectively take place, and closed porosity, referring to the fraction of the total volume with fluids or gases confined within the matrix (impermeable).

Understanding the morphology of the porosity is thus very important for groundwater, petroleum flow, and in the case of coal, surface and inherent moisture content entrapped in coal. It is a well established fact that coal is a porous substance and that both the pore size distribution and total pore volume vary, depending on a number of factors.

Various systems of classification of the pores have been proposed by different authors (van Krevelen, 1993). Consensus has been reached with regard to classifications resulting from high-resolution electron microscopy, where coal is characterized by a dual porosity consisting of macropore and micropore systems.

The micropore system consists of pores less than 2 nm in diameter and which occur as part of the matrix, while the macropore system is related to the fracture network designated by the cleat system, bedding planes, and surfaces (van Krevelen, 1993). Macroporosity refers to pores that are greater than 50 nm in diameter. Flow-through macroporosity is described by bulk diffusion. Mesoporosity refers to pores that have a diameter between 2 nm and 50 nm. Microporosity refers to pores that are smaller than 2 nm in diameter. Movement in micropores is by activated diffusion.

Lower rank high-volatile bituminous coals and sub-bituminous coals have a relatively high total porosity and a high proportion of intermediate pore sizes. High-rank bituminous coals have no intermediate sized pores and appreciably lower microporosity, while lignites on the other hand have high levels of macroporosity. Figure 14 illustrates the effect of coal

rank on porosity. Macropores predominate in the lower ranks, while geophysical factors relating to compaction and water expulsion gradually reduce the porosity in the higher ranks. The development of secondary porosity begins with the formation of micro- and mesopores at approximately the low-volatile bituminous coal rank designation, implying an increase in porosity due to progressive changes in the molecular structure through the higher ranks.

Porosity is related to the maceral composition, where microporous content is found predominantly in the vitrinite content and meso- to macroporous content predominates in inertinite (Gan *et al.*, 1972; Unsworth, Fowler, and Jones, 1989; Lamberson and Bustin, 1993; Levine 1993).

Coal porosity is also associated with cleats within the coal seams. Cleats are natural opening-mode fractures in coal beds. They usually occur in two sets that are, in most instances, mutually perpendicular and also perpendicular to the bedding. These fracture sets, and partings along bedding planes, impart a blocky character to coal (Figures 15 and 16). Cleats account for the predominant natural porosity and permeability paths in coal seams. Coal cleats are extensional fractures that formed, especially in the vitrain layers, as a result of active coalification processes and fluid pressure exerted during tectonic events (Close, 1991).

Vitrain/non-vitrain interbeds, which have different mechanical properties, were subjected to different strain magnitudes during these tectonic episodes, which also favoured fracture genesis. In the light of the effects of coalification on cleat development, Levine (1993) noted that porosity of coal is a function of molecular interactions. Levine's study suggested that cleat porosity is related to the compositional constituents, namely the macerals and minerals, as well as the maturity of the coal, which changes with the coalification process.

The relationship between porosity and carbon content was determined using laboratory tests on coal samples (Ettinger, 1960). The results showed that minimum porosity occurred at a carbon content of approximately 70 to 80%, representative of low-volatile bituminous to medium-volatile bituminous coal. Jones *et al.* (1988) found that the mechanical properties governing the apertures and frequency of cleats were related to coal type and rank. More recent work, however, has shown

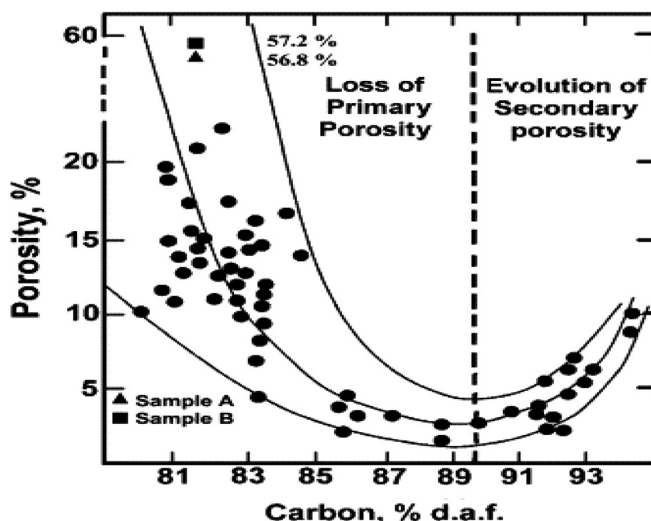


Figure 14—Relationship between coal porosity and coal rank (Gan, 1977; King and Wilkins, 1944; Levine, 1993)

Density – A contentious issue in the evaluation and determination of Resources and Reserves

that the lowest porosity occurs at a dry mineral matter-free fixed carbon content of approximately 89%, as shown in Figure 14 (King and Wilkins, 1944; Levine, 1993).

The cleats, however, contribute to the moisture storage capacity of the coals in addition to moisture storage within the micro- through macropores related to coal type maceral composition and rank.

One remarkable attribute of cleat formation is the extent to which they are developed in many coal beds of nearly all ranks in maturity. Cleats are typically much more intensely developed than fractures in adjacent non-coal rocks. Bright coal lithotypes (vitrain) generally have closer spaced cleats than dull coal lithotypes (durain).

Coals with low ash content tend to have smaller cleat spacings than coals with high ash content. Organic-rich shales also commonly have closely spaced fractures that resemble cleats. (Close, 1993) On a more diminutive scale, the sketches in Figure 18 shows examples of cleat formation and an indication of the extent of cleat formation in some hand samples.

It is evident that coal porosity, and as such relative permeability, can be highly variable. The movement of or saturation by moisture would in many instances be by diffusion,



Figure 15—Photograph of a 2.5 m mining horizon section illustrating the nature of the face and formation of cleats on a macro scale



Figure 16—Photograph of a hand sample illustrating cleats, especially noticeable in the vitrain layers of bright coal; note the blocky nature as a result of these smaller cleats



Figure 17—Vertical fissures and cleats

thus a reasonable amount of moisture would be retained in such a structure even if the large specimen were exposed to natural drying. This moisture is additional to the structurally bound moisture.

An interesting study was conducted by Wang (2007) on the influence of coal quality factors on seam permeability associated with coal bed methane production and cleat studies, which illustrates the reality of the cleat formation perfectly. The emphasis of this study was on the major cleats and involved the reduction of coal core samples to 40 mm cubes, which were treated with silicone gel in order to harden and preserve the samples. The cubes were then polished, removing the rough surfaces and resulting in a smooth shining surface on which the major cleats, spacing, length and apertures could be measured (Figure 19). This was illustrative of the major cleats regarded as connective and providing a major contribution to seam permeability as well as contributing to increased porosity.

It is against this background that the research was undertaken as it is believed that every effort should be made to obtain the correct information with regard to the true density of coal in order to establish a realistic evaluation of a given coal deposit.

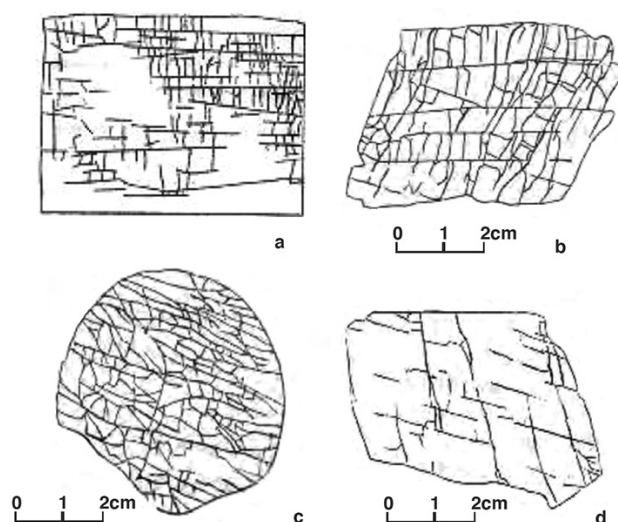


Figure 18—Sketches showing (a) parallel face cleats with general continuity and occasional discontinuity, (b) face cleats parallel and continuous, (c) a high-density cleat system in various directions, and (d) low-density parallel cleats (Fan, 1997)

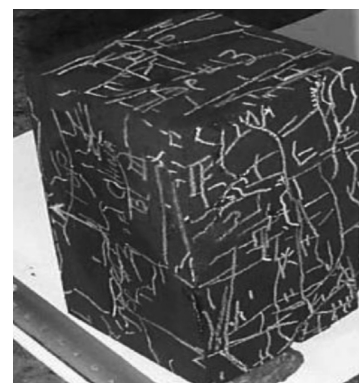


Figure 19—Photograph of a 40 mm coal cube displaying the major cleats infilled with silicone to contrast against the coal background and also to strengthen and retain the coal sample intact (Wang, 2007)

Density – A contentious issue in the evaluation and determination of Resources and Reserves

Geological losses

From the foregoing review of density, porosity, and moisture content, the major geological losses are related to porosity and moisture content of the matrix material. Quantification of these losses would enable a more accurate estimation of resource tonnages.

An evaluation of predicted product yields and the differences noted between the predicted values and actual plant production *via* the application of ash-adjusted density (AAD) initiated research concentrating mainly on the beneficiation aspects and in-house determined correlation factors that were applied to specific regions in the mine. This was based on the optimal yield and cut density prediction for semi-soft coking coal and power station middlings coal in the Waterberg Coalfield, Limpopo (Roux, 2012).

The results obtained allowed the negation of a collection of different correlation factors relating to the origin of the raw feedstock material. These factors were reduced to a single correlation factor specific to a particular beneficiation process. It was based on the beneficiation plant's capabilities and efficiency, the physical nature of the run-of-mine material, its reduction to a specific top size before processing, and the actual results obtained, irrespective of the origin of the material. The implementation of this methodology after the plant-specific correlation factor had been applied to the theoretically determined product yields improved the predicted values to such an extent that the beneficiation plant's products were conforming with the predicted values. (Roux, 2012).

The probability that the correlation factor could be removed entirely still existed, however, since the correlation factor, although plant-specific, was based on plant production results, and a deficiency equivalent to the difference between the plant-specific correlation factor and a 100% theoretical yield value determined from the cumulative wash table remained. This difference at the time was approximately 17.82%.

If this difference could be accommodated and negated then the reconciliation loop would be complete and it would support the values obtained from the geological model, resulting in increased confidence in the credibility of the data. Paramount in this evaluation was consideration of the relationships between coal density and porosity, with porosity and interrelated

permeability playing a major role in varying densities for the same volume of material.

Methodology

Three approaches to validate the determination of credible density values, namely, the revised AAD methodology (Roux, 2012), the evaluation of pure coal and mineral matter (Robeck and Huo, 2015), and the Australian Standard method (pycnometer or density bottle) were used.

Ash-adjusted density

The original theory with regard to the AAD methodology as outlined by Roux (2012) was based on distribution and cumulative frequencies of the float fraction values from a 31 000 sample data-set. This resulted in a linear regression for the ash/density relationship where $RD = 0.0136 \times \text{Ash\%} + 1.198$, giving an R^2 value of 0.99.

The sample data-set was re-evaluated by deriving descriptive statistics for each sample float fraction and regressions on the mean, median, and mode values to complement and enhance the earlier work on the data-set. The re-evaluated statistics for the ash content at the coal float fractions are presented in Table II.

The revised regression based on the median values (Figure 20) is:

$$\text{Absolute dry RD} = 0.0130 \times \text{Ash\%} + 1.2384$$

This gives a better result than the previously determined regression since the derived equation validates the petrophysical matrix density of bituminous coal as published by Schlumberger, where a matrix density for bituminous coal is given as 1.24 g/cm³, for anthracite 1.47 g/cm³, and lignite 1.19 g/cm³.

The first part of the equation represents the incremental indestructible mineral content of the sample, with the intercept being represented by a constant equivalent to the matrix density of a bituminous coal. The AAD value represents the absolute dry density of the float fraction. The expected air-dry density was approximated by including the effect of the inherent moisture content derived from proximate analysis.

The resultant density value was found to be slightly higher than the AAD value determined.

A reconstruction of the sample to *in-situ* relative density could then be calculated, provided that the free moisture content

Table II

Descriptive statistics results for float fractions analysed

	Ash 1.35 g/cm ³	Ash 1.40 g/cm ³	Ash 1.50 g/cm ³	Ash 1.60 g/cm ³	Ash 1.70 g/cm ³	Ash 1.80 g/cm ³	Ash 1.90 g/cm ³	Ash 2.00 g/cm ³	Ash 2.10 g/cm ³
Mean	7.34	13.51	20.22	28.48	35.96	42.32	48.15	53.32	57.08
Standard error	0.05	0.08	0.09	0.10	0.09	0.09	0.10	0.10	0.12
Median	6.99	14.06	21.00	29.20	36.41	42.61	48.60	53.70	57.67
Mode	6.10	16.00	21.70	29.90	37.60	44.00	51.00	52.70	59.10
Standard deviation	2.09	3.62	4.14	4.23	4.14	4.16	4.33	4.48	5.12
Sample variance	4.36	13.07	17.14	17.89	17.16	17.29	18.77	20.09	26.22
Kurtosis	3.03	0.52	0.14	-0.23	-0.30	-0.19	0.04	0.36	0.12
Skewness	1.29	0.17	-0.31	-0.26	-0.13	-0.15	-0.38	-0.46	-0.50
Range	17.22	26.23	25.40	27.50	27.96	30.70	29.10	31.80	31.61
Minimum	3.28	4.47	8.70	15.90	23.74	27.20	32.70	36.30	39.09
Maximum	20.50	30.70	34.10	43.40	51.70	57.90	61.80	68.10	70.70
Sum	14156.60	26103.04	39170.81	55259.82	69800.52	82064.53	92059.22	100987.23	107816.41
Count	1928	1932	1937	1940	1941	1939	1912	1894	1889
95% Confidence level	0.09	0.16	0.18	0.19	0.18	0.19	0.19	0.20	0.23

Density – A contentious issue in the evaluation and determination of Resources and Reserves

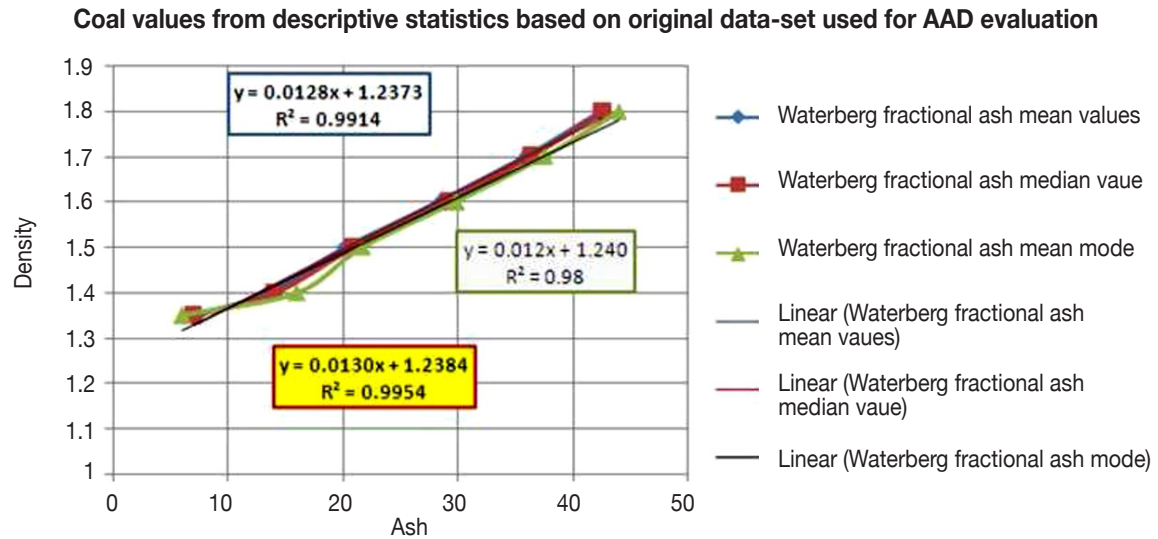


Figure 20—The revised regression based on descriptive statistic results obtained for each float fraction from the original data-set

and air- or gas-filled voids of an impeccably preserved sample are known.

Evaluation of pure coal and mineral matter for in-situ density determination (Robeck and Huo, 2015) - the Gray method

The proposed evaluation requires an estimation of mineral matter content, and the most commonly used method is the Parr formula (Rees, 1966).

$$M_d = 1.08 Ad + 0.55 S_{tot}$$

where S_{tot} = total sulphur (dry)

and the mineral matter ratio is determined by

$$r = \frac{1.08Ad + 0.55S_{tot}}{Ad}$$

An alternative, the Gray method in which M_d cannot exceed 100%, accounts for a wider range of mineral volatiles and reveals changes in mineral content with increasing ash.

This only requires specific energy (CV) and ash, and is the most robust, particularly for high-ash samples. The relationship between dry CV and mineral matter is given by:

$$E_d = E_{dmmf} \frac{100 - M_d}{100}$$

where

E_d = Specific energy, dry, expressed in MJ/Kg

E_{dmmf} = Specific energy, dry mineral matter free The mineral matter ratio is determined by

$$r = \frac{100 (E_{dmmf} - E_d)}{E_{dmmf} Ad}$$

The dry mineral matter-free CV is determined by:

$$E_{dmmf} = \frac{100 * (CV - 0.155)}{(100 * (Minh + 1.08) * (Ad + 0.555))}$$

Mineral matter content is then derived by:

$$Md = rAd$$

The determination of the air-dry density of the sample is then obtained from the equation:

$$\rho_{est} = \frac{100}{(a +) * M_d}$$

where coefficients a and b are determined by:

$$a = \left(\frac{Minh}{\rho_w} \right) + 100 - \left(\frac{Minh}{\rho_c} \right)$$

where ρ_c represents the matrix density of bituminous coal, 1.2384 g/cm³c and ρ_w is the density of water at 5°C, 1.0 g/cm³.

$$a = 100 - \left(\frac{Minh}{100} \right) * \left(\frac{\rho_c - \rho_m}{\rho_c * \rho_m} \right)$$

where ρ_m = density of the mineral matter (here 2.53 g/cm³ was used for Waterberg coals).

The individual densities of the samples can then be obtained from the following equations.

$$\rho_c = \frac{100}{a}$$

and

$$\rho_m = \frac{100}{a + (100 *)}$$

Australian Standard method (AS1038.21 Item 4)

The most common method used is the Australian Standard method (AS1038.21 Item 4) where the coal sample is pulverized to -212 µm, thereby removing fissures and some pores. It is then air-dried, retaining some (but not all) of its *in-situ* moisture, weighed, and submerged in a density bottle or volumetric flask. The amount of water displaced relates to the volume of the ground material, which is then divided by the mass to obtain the relative density, referred to as the standard relative density.

Research and evaluation results

Ash-adjusted density validated against laboratory-determined density

An exploration borehole, sampled and dispatched for analyses,

Density – A contentious issue in the evaluation and determination of Resources and Reserves

was treated in the normal way according to the standards followed by the accredited laboratory responsible for the analyses. In addition to the normal float/sink and proximate analyses, it was requested that the true relative density of each float fraction be determined using the density bottle method (Australian Standard method) at the same laboratory. These values were compared with AAD values obtained by application of the derived algorithm to ascertain the accuracy of the algorithm. The two sets of results, *i.e.* laboratory true density and AAD values, were found to be very close.

The 'true relative densities' of 741 float and sink fractions were determined according to the Australian Standard method, AS1038.21 Item 4. In the process of converting a coal sample to a ground, air-dried state the greatest change is noted in the volume, which has a greater effect on the relative density than the loss of mass. In this situation, the density trend would approximate the absolute density of the coal.

The float and sink wash data for the individual coal and shale samples from the exploration borehole was evaluated. The coal and shale samples were combined for the separate stratigraphic units' AAD-derived densities and the re-determined laboratory densities were compared and statistically evaluated at a 99.9% confidence level. The cumulative probability of the difference between the two measured data-sets showed a very positive result. The coal and shale sample data was then combined and re-evaluated statistically. The individual coal and shale results, as well as a combination of coal and shale results, are shown in Figure 21.

All three sets of values obtained at various confidence levels indicate a high level of accuracy. Since this evaluation is based on a comparison between AAD calculated values and laboratory-determined values, it is apparent that the AAD methodology can be used confidently for predictions of dry densities in coal assessments. Minor differences between the two data-sets (the AAD results and the density bottle results) are attributable to the inherent moisture content of the samples. The AAD values had not been corrected to accommodate the inherent moisture content, thus they represent an absolute dry matrix density, and if this correction is applied the values would be comparable with an air-dry density.

This research was confined to the crushed, air-dried $-13 + 0.5$ mm material that was sink/float separated to obtain a range of fractions for further analysis. The values pertinent to the true density of the matrix material were assessed by re-determination of the relative density through the application of the ash-adjusted density algorithm and then compared.

The samples require reconstruction to resemble the raw material prior to crushing. This needs the restoration of the sample to its original volume, which can be achieved by considering properties such as moisture content and porosity, both of which were altered during sample preparation when the sample was pulverized to $-212 \mu\text{m}$ for the pycnometer density determination.

Evaluation of pure coal and mineral matter for in-situ density determination (Robeck and Huo, 2015)

The air-dry relative density values for the exploration borehole samples were obtained by applying the Gray method. This pertained to the air-dry density of the samples because information on the free moisture content was not available. This approach was comparable to the AAD methodology since the AAD results refer to the absolute dry density of the samples (density excluding inherent moisture).

A chart similar to the 'Fish Diagram' developed by Robeck and Huo (2015) was populated with Waterberg coal data derived using both the Gray and Parr methods. As r increases on the y axis, the amount of mineral volatiles also increases (Figure 22). The relative position between zero and the 100% limit indicates the relative coal/mineral content. The area to the right of the 100% line is indicative of the amount of inorganic volatile matter (Robeck and Huo, 2015). Values below approximately 23% ash content are less reliable and may be approximated by the average of the Parr data-set at 1.12; the mean for the Gray data-set is 1.20.

Note that the Waterberg samples exhibit an abundance of kaolinite with minor silicates. Three sets of data – values derived from the AAD method, values from the Gray adapted method, and lastly the laboratory-determined density bottle values – were then plotted for comparative purposes.

The values determined from the AAD and Gray methods represent absolute dry (for AAD values) and air-dry densities. The AAD values have been adjusted from an absolute dry basis to an air-dry basis based on the inherent moisture content for a 100% yield so that all three data-sets are now comparable. Note that the matrix density of bituminous coal at 1.24 g/cm^3 and that of the mineral content at 2.53 g/cm^3 are the same as the values used in the AAD evaluation, and have been used in the Gray method. Trends established by the AAD and Gray methods correlate almost perfectly, with a slight divergence in the higher ash regimes, as shown in Figures 23, 24, and 25.

Note that the laboratory values up to 2.0 g/cm^3 are generally lower than both sets of calculated values. Although these

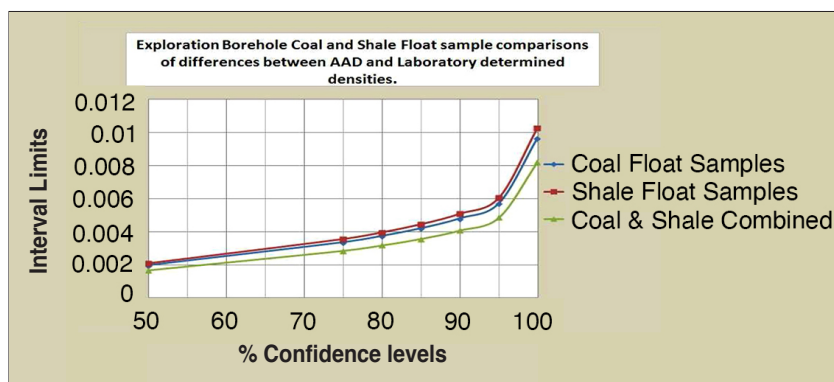


Figure 21 – Confidence level accuracies for coal, shale, and coal-shale combination

Density – A contentious issue in the evaluation and determination of Resources and Reserves

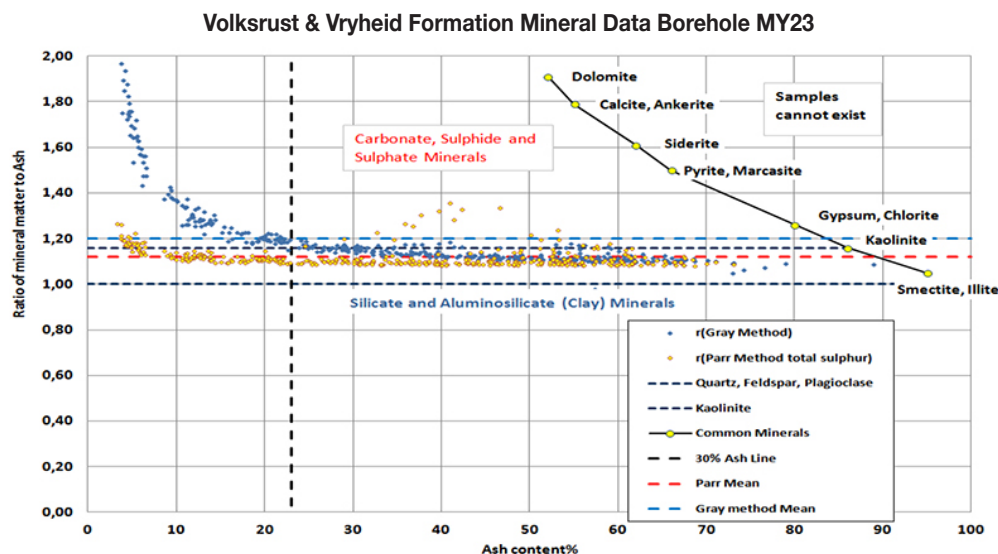


Figure 22—Diagram illustrating the ratio of mineral matter to ash vs. sample ash

Air dry float fractions ash/density comparison on combined Volksrust & Vryheid Formation Data

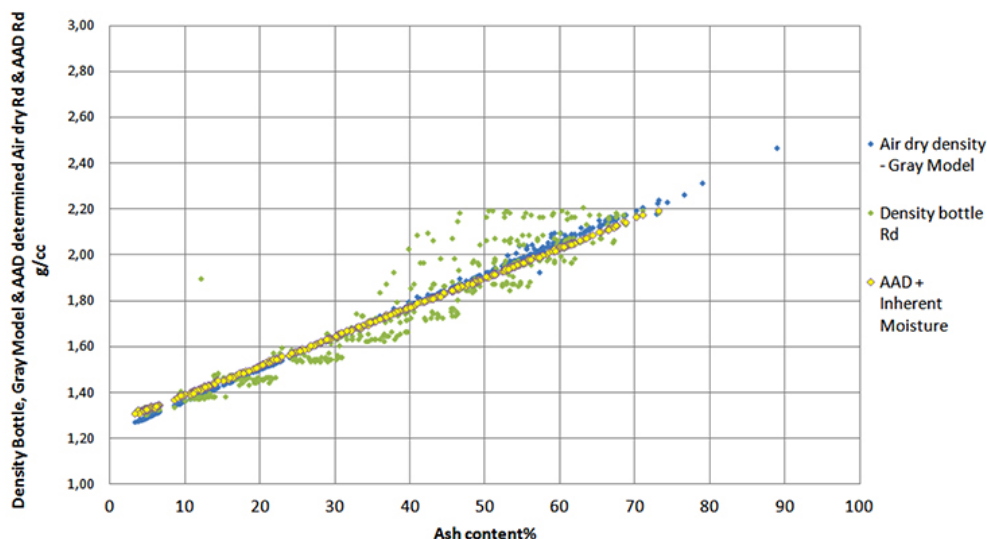


Figure 23—Plot of inherent moisture-adjusted AAD RD, Gray Method RD, and laboratory density bottle RD

AAD absolute dry float fractions ash/density comparison on combined Volksrust & Vryheid Formation Data

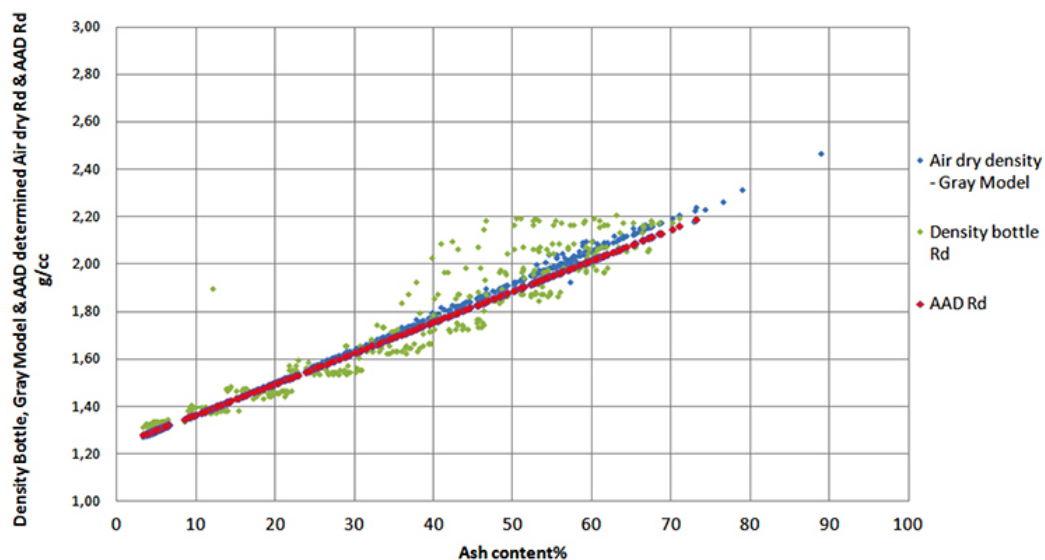


Figure 24—Plot of absolute dry density obtained from AAD against the Gray model and density bottle densities

Density – A contentious issue in the evaluation and determination of Resources and Reserves

Diff between Gray and AAD moist adjusted Rd		Diff between Gray method and AAD Rd	
Mean	-0,014	Mean	0,005
Standard Error	0,001	Standard Error	0,001
Median	-0,013	Median	0,002
Mode	0,000	Mode	0,000
Standard Deviation	0,016	Standard Deviation	0,011
Sample Variance	0,000	Sample Variance	0,000
Kurtosis	-0,946	Kurtosis	-0,697
Skewness	-0,141	Skewness	0,456
Range	0,075	Range	0,049
Minimum	-0,051	Minimum	-0,014
Maximum	0,024	Maximum	0,035
Sum	-5,766	Sum	1,909
Count	416	Count	416
Confidence Level(95,0%)	0,002	Confidence Level(95,0	0,001

Figure 25—Descriptive statistics for the differences between the Gray method and AAD moist-adjusted, as well as between Gray method and AAD

samples are air-dry, containing their inherent moisture, they are less dense than the calculated equivalents, implying an air-filled volumetric difference contributing to the lower density.

The calculations did not include estimations of *in-situ* moisture and the final estimation for an *in-situ* relative density. The absence of any data relevant to moisture content of the cores on recovery led to the determinations being terminated at an air-dry equivalent.

Variability of densities

In order to illustrate the variability of densities over a period of time a further set of samples was taken randomly from a borehole in the deeper part of the Waterberg Coalfield where the entire succession was well below the regional groundwater table. The purpose was specifically to test various density determinations, as well as helium pycnometry, in an attempt to justify the decision to terminate evaluations at an air-dry equivalent value.

The results are portrayed in Table III. The samples were not impeccably preserved; they had been exposed to atmospheric conditions for about two weeks after recovery from drilling and thus were partially dry. The field mass would therefore have been partially dry. The samples were sent to an external laboratory for specified relative density determinations, but this could not be done and the samples were returned and stored for approximately 7 months before being sent to another laboratory for helium pycnometry.

The first set of data was derived on an as-received basis. The samples were then dried at 105°C for 24 hours and re-tested, giving more representative air-dry results. The final set of data was determined after the samples had been re-submerged in water for 48 hours, presenting a different set of results.

This illustrates the susceptibility of the samples to moisture absorption from the ambient atmosphere and raises doubt with respect to densities other than air-dried densities for Reserve calculations. The variability of results obtained is directly related to the effective porosity of the samples and the ambient environmental and atmospheric conditions.

An example, following the practice with known and derived values evaluated for each of the mentioned methods, follows. In this case a sample of exploration core, 257 cm long with a cross-section of 117.81 cm², weighing 46.440 g on recovery, was used.

The initial data available was the mass in air, mass in water, and the calculated bulk (geometric) volume. There was no data relevant to total free moisture content since the core had not been impeccably preserved on recovery. A field specific gravity determination by the Archimedes principle was then done prior to the core being dispatched to an accredited laboratory for further analysis. The SG value obtained was used to represent the *in-situ* density of the core and in the determination of resource tonnages.

Returning to basic concepts in order to assess the differences, the basic equation of Density = Mass/Volume and variations of this equation were utilized to determine different values dependent on given variables.

The recovered mass of the core sample was 46.440 g and its bulk volume was 30 227 cm³, which gave a density of 1.53 g/cm³. The Archimedes-determined SG was 1.68 g/cm³. The most significant change here related to the mass of the sample; applying the density derived *via* Archimedes resulted in a calculated mass of 50.177 g, a 3.737 g difference. This is equivalent to approximately 7.5%, which can only be attributed to the moisture absorbed by the core during the hydrostatic determination. The difference in calculated volume and the original geometrical volume is also approximately 7.5%. Neither of these densities is suitable to use as an *in-situ* density value because the adventitious moisture content on retrieval is unknown.

The core was then dispatched to an accredited laboratory for further analysis. On reception the core was again weighed and the mass received recorded. It was then crushed to a -13 mm top size and screened to include the -13 mm and the +0.5 mm particles. The crushed material was air-dried under controlled conditions of temperature and humidity and once again weighed before float/sink analysis was done on the crushed material. The mass thus obtained was used in conjunction with the original volume, producing yet another density value, substantially less than the previously determined densities. In this case the air-dried mass of the -13 mm +0.5 mm material was 41.113 g (the calculated equivalent mass was 41.109 g) and the derived density was 1.36 g/cm³. This density was still not representative of the solid matrix because no mention was made of the -0.5 mm fraction after the screening had been done. This fraction's mass should have been included for the mass to be representative of the solid matrix within the overall measured volume of the core. Fortunately this value was available for this sample. The -0.5 mm mass was 2.990 g, thus taking the total to 44.103 g representing the air-dry mass of the material on which float and sink and proximate analyses were done. The revised density using the above mass would then be 1.46 g/cm³. If this density represents the particulate solid material of the matrix then its equivalent volume within the total core can be determined. Table IV illustrates the initial field and preliminary laboratory evaluation of mass, volume, and density.

The equivalent volume for an air-dry density is represented by 87% solids and 13% voids for this sample measured against the Archimedes-determined SG, assuming that the core was entirely saturated. Float/sink analysis at fixed density values ranging from 1.35 g/cm³, 1.40 g/cm³, and then at 0.1 g/cm³ intervals to a 2.20 g/cm³ float with a final sink value greater than 2.20 g/cm³ were then done. Each float fraction was then pulverized to -212 µm for the density bottle RD determination according to procedure AS1038.21 Item 4 and subsequent proximate analyses of each float fraction. The results are shown in Table V.

Density – A contentious issue in the evaluation and determination of Resources and Reserves

Table III

Results of randomly selected samples, illustrating the effects of absorption of atmospheric moisture, drying, and re-wetting through submergence in waters

Original data prior to submission to Anglo Lab for pycnometry										
Sample name	In-situ mass (kg)	In-situ mass (g)	Length (cm³)	Geometric volume (cm cubed)	Dry mass (kg)	Dry mass (g)	Field RD	RD gram/ ³ cubic cm³	Geometric volume (cm cubed)	Volume from pycnometry
Sample 1 (5)	1.527	1 527.00	36	1 134.00	1.5250	1 525.00	1.36	1.34	1134.00	1 133.33
Sample 2 (9)	1.283	1 283.00	29.5	929.25	1.2780	1 278.00	1.38	1.38	929.25	954.55
Sample 3 (9)	2.006	2 006.00	34	1 071.00	2.0040	2004.00	1.87	1.87	1 071.00	1 032.29
Sample 4 (1 ME)	1.671	1 671.00	29	913.50	1.6690	1669.00	1.83	1.83	913.50	1 039.87
Sample (5)	1.656	1 656.00	34	1 071.00	1.6540	1 654.00	1.5	1.54	1 071.00	993.90
Sample 1 (6)	0.919	919.00	17.5	551.26	0.9200	920.00	1.67	1.67	551.25	520.00
First set of data from Anglo Lab on samples received (untouched for period from June 2014 to January 2015)										
Folder No.	REPLNR	Order No	Sample name	Bulk relative density (g/cm³)						
187482	1	4362144_1	Sample 1 (5)	1.4						
187482	1	4362145_1	Sample 2 (9)	1.43						
187482	1	4362146_1	Sample 3 (9)	1.96						
187482	1	4362147_1	Sample 4 (1ME)	1.61						
187482	1	4362148_1	Sample 5	1.64						
187482	1	4362149_1	Sample 6	1.75						
187482	2	4362149_2	Sample 6R	1.73						
First set of data from Anglo Lab on samples received (untouched for period from June 2014 to January 2015)										
Folder No.	REPL NR	Order No	Sample name	Dry mass	Relative density (g/cm³)		Relative density (g/cm³)		Volume from pycnometry	
187482	1	4362144_1	Sample 1 (5)	1 496	1.4		1.32		1 133.33	
187482	1	4362145_1	Sample 2 (9)	1 260	1.43		1.32		954.55	
187482	1	4362146_1	Sample 3 (9)	1 982	1.96		1.92		1032.29	
187482	1	4362147_1	Sample 4 (1ME)	1 643	1.61		1.58		1 039.87	
187482	1	4362148_1	Sample 5	1 630	1.64		1.64		993.90	
187482	1	4362149_1	Sample 6	910	1.75		1.75		520.00	
187482	2	4362149_2	Sample 6R	910	1.73		1.74		522.99	
Samples submerged for 48+ hours, mass recorded after no dripping noted from samples										
Folder No.	REPL NR	Sample No	Sample name	Dry mass	Wet mass (g/cm³)		Nett mass (g/cm³)			
187482	1									
187482	1	4362144	Sample 1 (5)	1 510	1 560		50			
187482	1	4362145	Sample 2 (9)	1 270.1	1 310		39.9			
187482	1	4362146	Sample 3 (9)	1 996	2 040		44			
187482	1	4362147	Sample 4 (1ME)	1 654.1	1 716		61.9			
187482	1	4362148	Sample 5	1 643.3	1 684		40.7			
187482	2	4362149	Sample 6	915.8	934		18.2			
Comparativie table from dry to saturation after 48 hours										
Sample name	Dry mass	Wet mass	Difference	Volume	Dry Rd		Wet Rd		Moisture absorbed	
Sample 1 (5)	1 496	1 569	64	1 133.33	1.32		1.38		4.10%	
Sample 2 (9)	1 260	1 310	50	954.55	1.32		1.37		3.82%	
Sample 3 (9)	1 982	2 040	58	1 032.29	1.92		1.98		2.84%	
Sample 4 (1ME)	1 643	1 716	73	1 039.87	1.58		1.65		4.25%	
Sample 5	1 630	1 684	54	993.90	1.64		1.69		3.21%	
Sample 6	910	934	24	520.00	1.75		1.80		2.57%	

Table IV

Initial field evaluation of sample 14 from MY23

Sample No.	Lab mass	-13 mm mass	Total < 0.5 mm mass	Arch. SG	Thickness (cm)	Core volume	Field mass SG	Lab mass SG	-13 mm mass SG
Coal									
14	34620	30620	2387	1.58	202	23798	1.45	1.45	1.29
< 13 mm + < 0.5 mm mass		33007				23798	Air dry SG		1.39
Shale									
14S	11654	10493	603	1.98	55	6480	1.81	1.80	1.62
< 13 mm + < 0.5 mm mass		11096				6480	Air dry SG		1.71
Combined coal and shale -13 mm + 0.5 mm screened air dry material									
14	46274	41113	2990	1.68	257	30277	1.53	1.53	1.36
Combined coal and shale including -0.5 mm material									
14	46274	41113	2990	1.68	257	30277	1.53	1.53	1.36
Actual air dry mass incl < 0.5 mm	44103								1.46

Density – A contentious issue in the evaluation and determination of Resources and Reserves

Table V

Float/sink and proximate analyses results for the two separate components, coal and shale for Sample 14

Borehole BH ID	Sample	Type	Fraction type	RD 1	RD 2	Yield	Moisture	Ash	Volatiles	Sulphur	CV	Pycn. RD	AAD RD	-13 mm mass contribution	< -0.5 mm mass
Float/sink and other analyses performed on coal and shale portions of Sample 14 MY23															
Sample 14 MY23 Coal															
MY311LQ23	14	Coal	F	0	1.35	9.52	3.45	4.11	36.48	0.69	30.99	1.33	1.29	2916	
MY311LQ23	14	Coal	F	1.35	1.4	5.51	2.76	11.01	35.28	0.79	28.54	1.39	1.38	1687	
MY311LQ23	14	Coal	F	1.4	1.5	19.17	2.33	19.66	32.46	0.82	25.66	1.46	1.50	5868	
MY311LQ23	14	Coal	F	1.5	1.6	19.84	1.97	27.21	29.80	0.79	22.79	1.54	1.59	6076	
MY311LQ23	14	Coal	F	1.6	1.7	14.63	1.79	35.85	26.47	0.9	19.76	1.64	1.71	4478	
MY311LQ23	14	Coal	F	1.7	1.8	11.09	1.87	41.98	24.13	0.78	17.17	1.72	1.79	3395	
MY311LQ23	14	Coal	F	1.8	1.9	7.28	1.67	51.22	22.37	0.93	13.32	1.88	1.91	2229	
MY311LQ23	14	Coal	F	1.9	2	4.34	1.48	53.77	24.61	1.1	12.08	1.97	1.94	1330	
MY311LQ23	14	Coal	F	2	2.1	1.84	1.54	53.38	30.10	1.83	11.61	2.08	1.93	563	
MY311LQ23	14	Coal	F	2.1	2.2	1.48	1.90	52.57	31.66	4.18	11.25	2.17	1.92	454	
MY311LQ23	14	Coal	R		0.5		2.15	23.39	32.25	1.13	23.53		1.54		2387
MY311LQ23	14	Coal	S	2.2	9.99	5.30	2.05	56.53	31.68	13.16	9.22	2.63	1.97	1622	
														30620	
Sample 14 MY23 shale															
MY311LQ23	14	Shale	F	0	1.5	4.94	2.77	16.59	31.69	0.8	26.83	1.42	1.46	519	
MY311LQ23	14	Shale	F	1.5	1.6	3.40	2.29	30.92	26.59	0.68	21.71	1.57	1.64	357	
MY311LQ23	14	Shale	F	1.6	1.7	5.03	2.34	39.71	23.04	0.55	18.36	1.70	1.76	528	
MY311LQ23	14	Shale	F	1.7	1.8	6.32	2.10	47.65	20.91	0.4	15.45	1.79	1.86	663	
MY311LQ23	14	Shale	F	1.8	1.9	8.84	2.14	54.55	17.76	0.31	12.63	1.90	1.95	928	
MY311LQ23	14	Shale	F	1.9	2	8.68	2.21	60.17	16.25	0.29	10.19	2.00	2.02	911	
MY311LQ23	14	Shale	F	2	2.1	10.37	2.06	65.65	14.29	0.25	8.05	2.10	2.09	1089	
MY311LQ23	14	Shale	F	2.1	2.2	16.24	1.87	71.94	12.49	0.18	5.85	2.21	2.18	1704	
MY311LQ23	14	Shale	R		0.5		1.74	50.77	19.79	0.69	14.53		1.90	0	603
MY311LQ23	14	Shale	S	2.2	9.99	36.16	1.39	79.82	10.29	1.06	2.72	2.4	2.28	3794	
														10493	
Borehole BH ID	Sample	Type	Fraction type	RD 1	RD 2	Yield	Moisture	Ash	Volatiles	Sulphur	CV	Pycn. RD	AAD absolute dry RD	AAD air dry RD	Mass contribution
Coal and shale cumulative of Sample 14															
MY311LQ23	14	C&S Comp.	F	0	1.35	7.12	2.58	3.08	27.29	0.52	23.19	1.00	1.28	1.31	2929
MY311LQ23	14	C&S Comp.	F	1.35	1.4	4.12	2.06	8.23	26.40	0.59	21.35	1.04	1.35	1.38	1695
MY311LQ23	14	C&S Comp.	F	1.4	1.5	15.58	2.44	18.89	32.27	0.81	25.95	1.45	1.49	1.52	6407
MY311LQ23	14	C&S Comp.	F	1.5	1.6	15.70	2.05	28.15	28.99	0.76	22.52	1.55	1.61	1.64	6456
MY311LQ23	14	C&S Comp.	F	1.6	1.7	12.21	1.93	36.82	25.60	0.81	19.41	1.65	1.72	1.75	5019
MY311LQ23	14	C&S Comp.	F	1.7	1.8	9.89	1.93	43.41	23.32	0.68	16.74	1.74	1.80	1.84	4065
MY311LQ23	14	C&S Comp.	F	1.8	1.9	7.67	1.79	52.06	21.21	0.77	13.15	1.88	1.92	1.95	3155
MY311LQ23	14	C&S Comp.	F	1.9	2	5.44	1.67	55.38	22.51	0.90	11.60	1.98	1.96	1.99	2235
MY311LQ23	14	C&S Comp.	F	2	2.1	3.99	1.67	56.47	26.12	1.43	10.71	2.09	1.97	2.01	1639
MY311LQ23	14	C&S Comp.	F	2.1	2.2	5.20	1.89	57.45	26.84	3.17	9.89	2.18	1.99	2.03	2138
MY311LQ23	14	C&S Comp.	S	2.2	9.99	13.07	1.88	62.39	26.29	10.11	7.58	2.57	2.05	2.09	5374
															41113
MY311LQ23	14	C&S Comp.	R		0.5	0.00	2.05	30.29	29.11	1.02	21.26		1.63	1.67	2990
Total air dry mass Sample 14															44103
Borehole BH ID	Sample	Type	Fraction type	RD 1	RD 2	Yield	Moisture	Ash	Volatiles	Sulphur	CV	Pycn. RD	AAD absolute dry RD	AAD air dry RD	
Coal and shale cumulative of Sample 14															
MY311LQ23	14	C&S Comp.	F	0	1.35	7.12	2.58	3.08	27.29	0.52	23.19	1.00	1.28	1.31	
MY311LQ23	14	C&S Comp.	F	1.35	1.4	11.25	2.39	4.97	26.96	0.54	21.51	1.01	1.30	1.34	
MY311LQ23	14	C&S Comp.	F	1.4	1.5	26.83	2.42	13.05	30.04	0.70	24.51	1.27	1.41	1.44	
MY311LQ23	14	C&S Comp.	F	1.5	1.6	42.53	2.28	18.62	29.65	0.72	23.78	1.37	1.48	1.52	
MY311LQ23	14	C&S Comp.	F	1.6	1.7	54.74	2.20	22.68	28.75	0.74	22.80	1.44	1.53	1.57	
MY311LQ23	14	C&S Comp.	F	1.7	1.8	64.63	2.16	25.85	27.92	0.73	21.87	1.48	1.58	1.61	
MY311LQ23	14	C&S Comp.	F	1.8	1.9	72.30	2.12	28.63	27.21	0.74	20.95	1.52	1.61	1.65	
MY311LQ23	14	C&S Comp.	F	1.9	2	77.74	2.09	30.51	26.88	0.75	20.29	1.56	1.64	1.67	
MY311LQ23	14	C&S Comp.	F	2	2.1	81.73	2.07	31.77	26.84	0.78	19.83	1.58	1.65	1.69	
MY311LQ23	14	C&S Comp.	F	2.1	2.2	86.93	2.06	33.31	26.84	0.93	19.23	1.62	1.67	1.71	
MY311LQ23	14	C&S Comp.	S	2.2	9.99	100.00	2.04	37.11	26.77	2.13	17.71	1.74	1.72	1.76	
MY311LQ23	14	C&S Comp.	R		0.5	0.00	2.05	30.29	29.11	1.02	21.26		1.63	1.67	

Density – A contentious issue in the evaluation and determination of Resources and Reserves

The proximate analyses shown in Table V were composited into a representative wash table of coal and shale combined. This was then cumulated to represent the effect of each additional yield from the basic 1.35 g/cm³ through to the 2.20 g/cm³ sink value. The AAD algorithm was applied to each float fraction to determine the absolute dry density and then corrected to an air-dry density by taking the inherent moist content into account. The density bottle values were also included in the wash tables for comparative evaluation. A summary of the masses, volumes, densities, and perceived percentage solids and voids for the varying densities determined is displayed in Table VI.

From the foregoing, very little difference is evident between the methods utilizing the analytical data. Densities of 1.45 g/cm³ to 1.46 g/cm³ were obtained using an average correction factor of 0.83 for the solid matrix, which implies that the effective porosity of this sample is approximately 17%.

Figure 26 shows the volumetric differences by the different methods applied. The first three, namely field mass, Archimedes, and laboratory air-dried densities, are all based on the original

bulk volume of the core sample and show very little to no variation, whereas the values derived from AAD on raw analysis, AAD on cumulative density, pycnometry (density bottle), and finally the Gray method are on average 17% lower than the geometrical volume.

If the original laboratory mass of 46.274 g and the determined air-dry density of 1.46 g/cm³ are taken into account, the volume to support this density would be 31.695 cm³, which is 1.418 cm³ greater than the original geometric volume (30.277 cm³) and by implication suggests more core than the original. The original core length was 257 cm and the cross-section 117.81 cm², therefore the extra volume would represent approximately 12 cm more core, increasing the original length to 269 cm. Since the core cannot stretch or grow, the only logical explanation is that the additional volume represents the voids/porosity of the solid matrix and that the solid matrix within the confines of the geometric volume is therefore equivalent to 100% less the depicted void volume, in this case 17%, thus the solid matrix is only 83% of the total volume (Figure 27).

Table VI						
Perceived percentage solids and voids based on various density determination methods. Combined coal and shale						
Determination method	Mass g	Volume cm³	Density g/cm³	Perceived % solids	Possible % voids	Mass loss from original field mass to other measured masses
Field and preliminary laboratory evaluation of perceived solids and voids						
Archimedes	46300	27560	1.68	0.91	0.09	26
Field mass/volume	46300	30277	1.529			
Lab mass./volume	46274		1.528			
Determination method	Mass g	Volume cm³	RD	% Solids	Possible % voids matrix	
Laboratory sample preparation evaluation of perceived solids and voids						
–13 mm – 0.5 mm mass/volume	41113	30277	1.358	0.81	0.19	5187
Air dry mass including < 0.5 mm/volume	44103		1.46	0.87	0.13	2197
Determination method	Mass g	Volume cm³	RD	% Solids	Possible % voids matrix	Air-dry RD derived from RD x % solid matrix
Validation of solid matrix RD based on pycnometer, AAD results and grey method						
Pycnometer RD1111.74	44103	25347	1.74	0.84	0.16	1.457
Absolute dry AAd RD			1.72	0.85	0.15	1.457
Air dry AAD RD			1.76	0.83	0.17	1.457
Gray method RD			1.75	0.83	0.17	1.460

VOLUMETRIC DIFFERENCES TO SUPPORT DERIVED DENSITIES FOR THE MATRIX

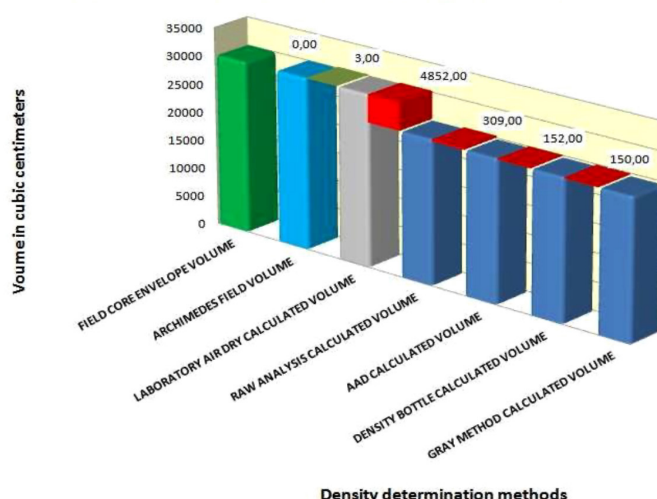


Figure 26—Volumetric differences based on the densities obtained from the different methods

Density – A contentious issue in the evaluation and determination of Resources and Reserves

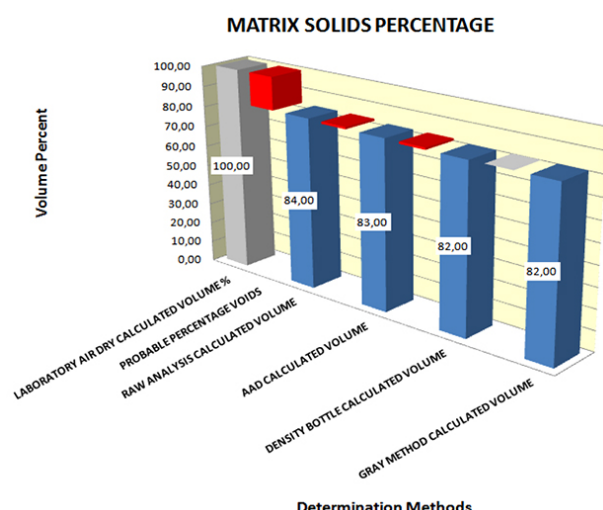


Figure 27—Solid matrix representation of values derived from the displayed determination methods

If the densities determined from the various methods were, however, used to calculate *in-situ* tonnages without corrections related to possible geological losses as determined by the volumetric evaluations applied, the net result would be substantially overestimated values (Table VII).

The overestimation is determined by the final percentage by which the calculated value exceeds the mass of the measured air-dry material, *i.e.* the Archimedes-calculated mass of 50.865 g measured against 44.103 g results in an overestimation of 15.07%. It is also apparent that the field mass volume contains a fair percentage of moisture.

It is of paramount importance that the methods under consideration are fully understood and that the AAD evaluation on the proximate analytical values needs to be adjusted to account for the inherent moisture of the coal, since the AAD gives an absolute dry density for the coal. The inherent moisture content determined for Waterberg coals is between 1.5% and 2.5%, which taken into account will slightly increase the determined density values, making them comparable with both the density bottle values and the Gray determinations. The sample then needs to be restored to its original volume and the void to solid ratio determined in order to get a representative air-dry relative density.

Production reconciliation

From a mining production and reconciliation perspective two examples, one from the Volksrust Formation and the second from the Vryheid formation, were dealt with. These two scenarios are depicted in the locality map shown in Figure 28, showing the positions of the mining strips, blocks, and surrounding exploration boreholes from which the basic information with regard to mining block densities and expected run of mine tonnages were obtained.

The same approach using the basic density equation was used in this evaluation. The masses relate to tonnages, the volumes in cubic metres to the material mined, and the initial densities allocated to the areas as well as the derived densities represented by the surveyed volumes and reported tonnages. Table VIII represents data from mining horizon bench 3 which is in the Volksrust Formation. Material from this bench is beneficiated for both a semi-soft coking coal and a power station product.

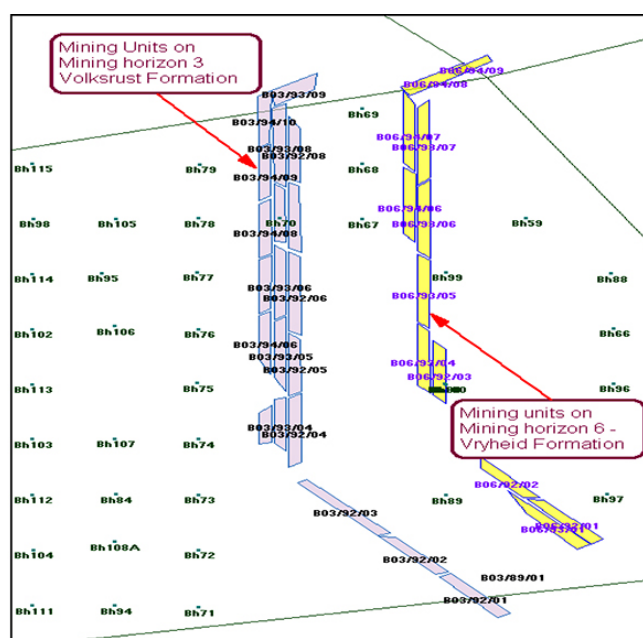


Figure 28—Locality map illustrating the respective mining strips, mining units, and mining horizons evaluated with locations of boreholes spread over the entire area

Table VII

Overestimation of core mass as a result of solid to void ratios

Determination method	Density g/cm ³	Volume cm ³	Actual solids volume cm ³	Voids volume cm ³	% voids	
Air dry mass including < 0.5 mm/volume	1.46	30277	25251	5026	16.60%	Based on average calc values from pycnometer, AAD and Gray methods. RD
Pycnometer RD	1.74		25347	4930	16.28%	
Air dry AAD RD	1.76		25130	5147	17.00%	
Gray method RD	1.75		25130	5147	17.00%	
Average for calculated values	1.75		25130	5147	17.00%	
Determination method	Density g/cm ³	Volume cc	Mass in grams = RD x volume	% Over estimation		
Archimedes	1.68	30277	50865.36	15.07%		
Air dry mass including < 0.5 mm/volume	1.46		44204.42			

Density – A contentious issue in the evaluation and determination of Resources and Reserves

Table VIII

Mining blocks on bench 3 (Volsrust Formation) with model-assigned areas, volumes, and predicted tonnages based on raw density values allocated to the various blocks as well as the information pertinent to these blocks when they were staked for drilling and blasting prior to mining

Block No.	Seam	Model area	Model thick	Model volume	Raw RD	Model report In-situ tons	Survey staked area	Seam thickness	Staked volume	Survey RD	Survey staked tons
B03/92/01w	B3	12 536.00	17.07	213 989.52	1.84	393 663.00	12 044.00	16.46	198 286.41	1.84	364 847.00
B03/92/02	B3	10 866.00	16.53	179 614.98	1.83	328 962.00	11 285.00	17.19	193 967.76	1.83	354 961.00
B03/92/03	B3	15 701.00	16.14	253 414.14	1.83	462 557.00	16 390.00	16.68	273 312.57	1.83	500 162.00
B03/92/04	B3	11 903.00	16.41	195 328.23	1.88	366 843.00	14 980.00	16.06	240 594.15	1.88	452 317.00
B03/92/05	B3	12 923.00	16.22	209 611.06	1.88	393 827.00	12 269.00	16.49	202 369.68	1.88	380 455.00
B03/92/06	B3	15 102.00	16.79	253 562.58	1.87	474 963.00	16 835.00	16.73	281 675.94	1.87	526 734.00
B03/93/04	B3	9 958.00	16.35	162 813.30	1.88	305 877.00	10 352.00	15.19	157 197.86	1.87	293 960.00
B03/93/05	B3	13 529.00	16.64	225 122.56	1.88	423 671.00	13 922.00	16.28	226 670.21	1.88	426 140.00
B03/93/06	B3	13 448.00	16.60	223 236.80	1.86	415 800.00	14 861.00	16.67	247 722.46	1.87	463 241.00
B03/93/07	B3	13 447.00	16.32	219 455.04	1.86	407 429.00	12 136.00	17.15	208 161.62	1.85	385 099.00
B03/93/08	B3	17 009.00	12.56	213 633.04	1.82	387 763.00	16 273.00	15.28	248 676.67	1.80	447 618.00
B03/93/09	B3	10 618.00	15.32	162 667.76	1.81	293 717.00	10 797.00	14.20	153 329.44	1.80	275 993.00
B03/94/04	B3	7 284.00	16.43	119 676.12	1.88	225 131.00	7 219.00	14.42	104 123.94	1.88	195 753.00
B03/94/06	B3	11 218.00	16.73	187 677.14	1.88	353 566.00	11 645.00	15.37	179 025.00	1.88	336 567.00
B03/94/07	B3	11 218.00	16.59	186 106.62	1.86	346 646.00	11 429.00	15.85	181 136.56	1.86	336 914.00
B03/94/08	B3	11 218.00	16.40	183 975.20	1.86	341 774.00	11 429.00	16.35	186 856.45	1.86	347 553.00
B03/94/09	B3	11 218.00	12.42	139 327.56	1.85	257 126.00	11 297.00	15.14	170 982.70	1.85	316 398.00
B03/94/010	B3	11 218.00	14.67	164 568.06	1.81	297 585.00	10 673.00	15.45	164 919.89	1.81	298 505.00
		220 414.00	15.85	3 493 779.71	1.85	6 476 900.00	225 836.00	16.02	3 619 009.31	1.85	6 703 137.00

Table IX

The same blocks as in Table VIII with as-mined values and the final survey reported results

Block No.	SEAM	As mined values at same basis					Survey measured data			
		As-mined area	As mined bench thickness	As mined volume	Equivalent as-mined In-situ tons	Model raw RD	Surveyed area	Survey thickness	Survey volume	Surveyed tons
B03/92/01	B3	11 348.64	16.46	186 838.38	343 782.62	1.84	10 945.42	17.07	186 838.38	274 173.58
B03/92/02	B3	8 155.14	17.29	140 986.92	258 006.07	1.83	8 529.15	16.53	140 986.92	223 129.73
B03/92/03	B3	19 037.82	16.38	311 755.13	570 511.88	1.83	19 315.68	16.14	311 755.13	478 641.71
B03/92/04	B3	14 423.51	16.66	240 310.45	451 783.64	1.88	14 644.15	16.41	240 310.45	379 294.56
B03/92/05	B3	9 794.55	16.19	158 616.71	298 199.41	1.88	9 779.08	16.22	158 616.71	246 191.78
B03/92/06	B3	13 455.32	16.13	217 055.40	405 893.59	1.87	12 927.66	16.79	217 055.40	322 471.29
B03/93/04	B3	6 693.13	15.09	100 967.70	189 819.27	1.88	6 175.39	16.35	100 967.70	144 819.98
B03/93/05	B3	17 134.02	15.98	273 826.30	514 793.45	1.88	16 455.91	16.64	273 826.30	408 835.50
B03/93/06	B3	13 487.42	16.27	219 430.95	408 141.56	1.86	13 218.73	16.60	219 430.95	330 768.83
B03/93/07	B3	1 108.46	16.65	18 458.52	34 332.84	1.86	1 131.04	16.32	18 458.52	28 968.07
B03/93/08	B3	1 064.31	14.98	15 944.98	29 019.86	1.82	1 269.50	12.56	15 944.98	28 623.02
B03/93/09	B3	1 463.42	14.30	20 928.50	37 880.58	1.81	1 366.09	15.32	20 928.50	29 240.23
B03/94/04	B3	1 074.37	13.82	14 851.66	27 921.12	1.88	903.94	16.43	14 851.66	19 425.37
B03/94/06	B3	8 223.62	15.27	125 603.81	236 135.17	1.88	7507.70	16.73	125 603.81	178 261.57
B03/94/07	B3	7 958.93	15.95	126 935.76	236 100.51	1.86	7 651.34	16.59	126 935.76	187 686.50
B03/94/08	B3	5 000.76	16.45	82 259.17	153 002.05	1.86	5 015.80	16.40	82 259.17	126 897.93
B03/94/09	B3	4 941.20	15.34	75 774.38	140 182.61	1.85	6 101.00	12.42	75 774.38	143 125.12
B03/94/10	B3	6 493.27	15.95	103 581.04	187 481.69	1.81	7 060.74	14.67	103 581.04	168 577.13
		150 857.88	16.14	2 434 125.76	4 522 987.95	1.86	149 998.33	16.23	2 434 125.76	3 719 131.90

In Table X, overestimation percentages are attributable to completely different areas, bench thicknesses, densities, and volumes planned and staked as opposed to the raw material actually mined. The most important fact, however, lies between the as-mined data and the surveyed data. In Table XI the areas, volumes, bench thicknesses, and relative densities for the model, staked, and as-mined scenarios have been equalized in order to compare the four scenarios on the same basis. The only difference is in the tonnage for the surveyed material and its resultant density. This shows a difference of 17.41%, which could be attributable to the voids in the matrix, implying that the solid matrix contributing to the final density is only 82.59%.

The second evaluation represents data from bench 6 in the Vryheid Formation. This material is mined, crushed and screened, and dispatched directly as a power station product.

Summary

Basic field and preliminary laboratory density determinations are valueless unless the core is impeccably preserved and its moisture content determined. If this has not been done the air-dry density should be validated through the evaluation of alternative methods, including pycnometry, application of AAD, and the Gray method. When using the Gray method it is advisable to use the inherent moisture content determined through proximate

Density – A contentious issue in the evaluation and determination of Resources and Reserves

analysis, the reason behind this being that Robeck and Hoe (2015) used averaged total moisture content in their evaluations. This may be from actual analyses on impeccably preserved core where moisture determinations were done.

Density determinations on the selected sample chosen for the theoretical evaluation after the –13 mm +0.5 mm and the –.5 mm air-dry mass divided by original geometric volume include:

- Australian Standard method, AS1038.21 Item 4

- The Gray method (Robeck and Huo, 2015)
- Ash-adjusted density (Roux, 2012).

These three methods all require the pulverization of the air-dried sample to –212 µm, leading to a significant loss in volume. Results obtained from the Gray method (using proximate analyses results for inherent moisture content) displayed a 0.01 g/cm³ density difference, slightly higher than the pycnometer and AAD results. Applying the same principle with regard to changing volumes, factors for the solid matrix were on average 0.83 (83% of the total sample) and voids 0.17 or 17%. These factors applied to the determined densities gave an air-dry density of 1.46 g/cm³ for the sample evaluated. This volumetric difference is a geological loss as a result of the matrix porosity of the material.

From a physical mining perspective, where more than a single sample was composited to represent a mining horizon bench, the reconciliation of tonnages hauled and the volumes of material extracted for the two scenarios evaluated also gave results within the same range as those obtained from laboratory and theoretical evaluations.

The first scenario, based on bench 3 production, shows a difference of 17.41% attributable to the voids in the matrix, which implies that the solid matrix contributing to the final density is only 82.59%. The second scenario, bench 6, resulted in a void percentage of 17.89% and a solid matrix percentage of 82.11%.

It is thus considered that a change of volume equation, given reliable input, will enable the determination of a more credible air-dry density of coal which can then be adjusted to accommodate adventitious moisture representative of *in-situ* conditions if accurate moisture determinations are done on impeccably preserved samples. Alternatively, the laboratory air-dry density should be used for Resource and Reserve calculations. This air-dry value should include both the mass of the screened –13 +0.5 mm as well as the mass of the –0.5 mm material.

Conclusions and recommendations

Field samples

1. If samples are not sealed and impeccably preserved in order

Table X

Summaries of the weighted averages for the four data-sets relevant to the foregoing mining units, depicting tonnage differences and overestimation percentages

	Summary of initial reported values				
	Area	Thick	RD	Volume	Tonnage
Model	220 414.00	15.84	1.85	3 491 357.76	6 459 011.86
Staked	225 836.00	16.02	1.85	3 617 892.72	6 693 101.53
As mined	150 858.00	16.14	1.86	2 434 848.12	4 522 987.95
Surveyed	149 998.00	16.23	1.53	2 434 125.76	3 719 131.91
Model to surveyed tonnage difference					2 739 879.95
Model % overestimation					60.84%
Staked to surveyed tonnage difference					2 973 969.63
Staked % overestimation					44.43%
A-mined tonnage difference					803 856.04
As-mined % overestimation					17.77%

Table XI

Comparison of planning, survey, and mining data-sets on the same basis

	Calculated values for surveyed area and volume				
	Area	Thick	RD	Volume	Tonnage
Model	149 998.33	16.23	1.85	2 434 125.76	4 503 132.66
Staked	149 998.33	16.23	1.85	2 434 125.76	4 503 132.66
As mined	149 998.33	16.23	1.85	2 434 125.76	4 503 132.66
Surveyed	149 998.33	16.23	1.53	2 434 125.76	3 719 131.90
As-mined tonnage difference					784 000.76
As-mined % overestimation					17.41%

Table XII

Mining blocks on bench 6 (Vryheid Formation) with model-assigned areas, volumes, and predicted tonnages based on raw density values allocated to the various blocks as well as the information pertinent to these blocks when they were staked for drilling and blasting prior to mining

Block No.	Geological model allocated values						Survey staked data				
	Model area	Model thick	Model PS coal yield	Model volume	Model report <i>in-situ</i> tons	Archimedes raw RD	Survey staked area	Survey staked tons	Survey RD	Calculated thickness	Staked volume
B06/92/01	13 651	4.22	100	57 607.22	95 964	1.67	12 400	78 881	1.67	3.81	47 234
B06/92/02	10 222	4.01	100	40 990.22	67 541	1.65	10 491	64 340	1.65	3.72	38 994
B06/92/03	12 746	4.03	100	51 366.38	84 734	1.65	11 282	54 038	1.65	2.90	32 750
B06/93/01	14 030	4.17	100	58 505.1	97 144	1.66	13 849	84 206	1.66	3.66	50 727
B06/93/04	14 285	4.02	100	57 425.7	94 216	1.64	12 892	69 008	1.63	3.28	42 336
B06/93/05	14 285	4.01	100	57 282.85	93 793	1.64	14 336	90 889	1.64	3.87	55 420
B06/93/06	14 285	4.04	100	57 711.4	93 645	1.62	15 095	89 224	1.62	3.65	55 077
B06/93/07	14 281	4.07	100	58 123.67	94 639	1.63	16 128	97 345	1.63	3.70	59 721
B06/93/08	5 216	3.94	100	20 551.04	33 624	1.64	2 819	17 546	1.64	3.80	10 699
B06/94/06	14 285	4.04	100	57 771.4	93 832	1.63	14 432	107 375	1.63	4.56	65 874
B06/94/07	14 281	3.96	100	56 552.76	92 410	1.63	14 684	98 621	1.63	4.12	60 504
B06/94/08	8 987	3.97	100	35 678.39	58 352	1.63	11 112	69 594	1.63	3.84	42 696
B06/94/09	7 500	4	100	30 000	48 860	1.63	5 715	26 638	1.63	2.86	16 342

Density – A contentious issue in the evaluation and determination of Resources and Reserves

Table XIII

Bench 6 blocks with as-mined reported values as well as the final survey results

Block No.	As mined reported data/Model					Model	Survey measured data		Despatch reported tonnages		
	Seam	As-mined area	As-mined bench thick	As-mined volume	Equivalent as-mined <i>in-situ</i> tons	Archimedes raw RD	Surveyed volume	Surveyed tons	GG3	GG2	Total despatch tons
B06/92/01	Bench 6	12 049	3.51	42 284	70 614	1.67	42 284	70 614	109 727	489	110 217
B06/92/02		10 926	3.92	42 797	70 614	1.65	42 797	70 614	82 095	1 309	83 404
B06/92/03		3 256	2.70	8 800	14 520	1.65	8 800	14 520	91 196	1 476	92 672
B06/93/01		31 934	3.56	113 775	188 867	1.66	113 775	188 867	56 746	813	57 559
B06/93/04		15 018	3.18	47 815	78 417	1.64	47 815	77 938	57 176	1 151	58 328
B06/93/05		10 751	3.47	37 261	61 108	1.64	37 261	61 108	70 092	1 633	71 725
B06/93/06		36 800	2.85	104 832	169 828	1.62	104 832	169 828	75 194	661	75 855
B06/93/07		15 273	3.10	47 390	77 246	1.63	47 390	77 246	77 423	1 194	78 616
B06/93/08		1 241	3.20	3 964	6 501	1.64	3 964	6 501	100 049	1 194	101 242
B06/94/06		69 319	2.26	1 569 70	255 861	1.63	156 970	255 861	51 522	3 447	54 968
B06/94/07		5 791	2.82	16 332	26 621	1.63	16 332	26 621	51 522	1 799	53 321

Table XIV

Comparison of planning, survey, and mining data-sets

	Summary of reported values				
	Area	Thick	RD	Volume	Tonnage
Model	15 805 4	4.05	1.64	63 950 6	10 487 24
Staked	15 523 5	3.73	1.64	57 837 3	94 770 5
As mined	21 235 7	2.93	1.64	62 222 0	102 019 6
Surveyed	21 236 2	2.93	1.64	62 222 0	10 197 18
Despatch					
Probable voids			17.89%		
Solid matrix			82.11%		

to retain the free moisture neither Archimedes nor field mass/volume density determinations are suitable for Resource and Reserve determinations based on so-called *in-situ* conditions. Moisture loss or gain as a result of exposure to atmospheric conditions or absorption during hydrostatic testing for SG determination will lead to erroneous results not representative of the sample in its *in-situ* state. If the sample is sealed on recovery, the densities determined by these methods should be almost identical. Corrections to convert to an air-dry density can then be done when the free moisture content has been determined.

- The mass of the initial laboratory-crushed air-dried state, including both the –13 +0.5 mm fraction and the –0.5 mm fraction, can be used over the original geometric volume to give an indication of the probable air-dry density of the sample, provided that the crushed material has been properly air-dried under controlled temperature and humidity, ensuring a credible value for the air-dried material.

Laboratory-prepared samples

- The density of float/sink fractions, air-dried, and pulverized to –212 µm determined by applying the Australian Standard method AS1038.21 Item 4 can be composited to give a representative air-dry density of the sample from the particles in the solid matrix.
- The AAD methodology can be applied to the proximate ash content data to determine an absolute dry density of the sample, which should then be adjusted to take the inherent moisture content into consideration to provide an equivalent air-dry density.

- The Gray method, proposed by Robeck and Huo, can also be used to determine an equivalent air-dry density for the sample. Robeck and Huo, however, oppose the use of the ash component since it is a product of combustion and excludes possible mineral volatiles. These mineral volatiles include H₂O of hydration, CO₂, SO₂, salts (*e.g.*, Cl), carbonates, and sulphides (Ward, 1984). As a result, the remaining ash (solid residue) underrepresents the original mineral matter. For this reason, sample ash almost never reaches 100%, even in samples lacking carbonaceous material.
- The greatest loss of mineral volatiles relates to water loss as a result of vaporization coupled with minor amounts of the aforementioned volatiles.
- The density values obtained from these laboratory procedures all need to be related to the original geometric or envelope (bulk) volume, because the total volume of the sample has been dramatically reduced as a result of pulverization. The mass of sample if properly air-dried, however, should remain the same.
- Ash-adjusted density with a correction applied to account for inherent moisture and then reconstructed to be accommodated within the original volume gives a reliable air-dry density and requires the least analytical data to acquire the desired result. These values have all been found to be within the 95–99% confidence range.

It is recommended that *Resource and Reserve tonnages be reported on an air-dry basis. Water and voids do not generate revenue.* The air-dry density gives credible results with respect to the actual resource material. If the moisture content in the matrix of the resource material is higher, the budgeted tonnages calculated on the air-dry basis would be more conservative, negating the possibility of overestimation of the actual Resource.

Resource and Reserve values can be adjusted to reflect an averaged free moisture content, enhancing planning and scheduling with regard to probable tonnages *in situ* in the specific environment being evaluated. This may be accomplished through the evaluation of downhole geophysical logs, specifically the density log. After correlation to identify the zones and samples, comparisons of log densities with AAD densities for the same samples can be made. The differences noted would be indicative of the probable moisture or void content in the samples.

One of the biggest influences with regard to fluctuating tonnages and varying *in-situ* densities can be attributed to

Density – A contentious issue in the evaluation and determination of Resources and Reserves

the movement of groundwater in relation to the material being evaluated. Depleting groundwater levels will result in lower tonnages as the groundwater drains from the porous material, while increased groundwater levels could saturate the material through absorption thereby greatly increasing the *in-situ* tons of raw material.

The use of air-dry densities in order to derive Resource and Reserve tonnages allows a very conservative approach. It is also the basis on which product data extraction is calculated, therefore any excesses measured in a mining operation can be adjusted to accommodate possible increases in free moisture content of the material being mined. This can be accommodated in the mining loss/gain factors applied to mineable tonnages.

References

- AMERICAN SOCIETY FOR TESTING AND MATERIALS. 1994. Compilation of ASTM Standard Definitions. 8th edn. West Conshohocken, PA.
- ANDERSON, G. 1975. Coring and Core Analysis Handbook. Petroleum Publishing Company, Tulsa, AZ.
- BRITISH STANDARD BS 2955. 1991. Glossary of Terms Relating to Particle Technology. British Standards Institution, London.
- CLOSE, J. 1993. Natural fractures in coal. *Hydrocarbons from Coal*, Law, B.E. and Rice, D.D. (eds). AAPG Studies in Geology, vol. 38. pp. 119–132.
- CRAIN, R. 2003. The new role of petrophysics in geophysical interpretation. *CSEG Recorder*, vol. 28, no. 7. <https://csegrecorder.com/articles/view/the-new-role-of-petrophysics-in-geophysical-interpretation>
- CRAIN, R. 2010. Petrophysical Handbook. Rocky Mountain House, AB, Canada.
- DREYER, J.C. 1991. Waterberg Coalfield: Geology, resources, mining and products. (Abstr.). *Proceedings of the Conference on South Africa's Coal Resources*, Witbank, 6–9 November. Geological Society of South Africa, Johannesburg.
- DREYER, J.C. 1994. Total utilization of the coal resource: The Grootegeluk experience. *Journal of the South African Institute of Mining and Metallurgy*, vol. 94. pp. 153–164.
- FALCON, L.M. 1987. The complexities of coal. *Review; Gold Fields of South Africa*. pp. 64–67.
- FALCON, R.M.S. 1986. Classification of coals in Southern Africa. *Mineral Deposits of Southern Africa*, vol. 2. Anhaeusser, C.R. and Maske, S. (eds.). Geological Society of South Africa, Johannesburg. pp. 1899–1921.
- GAN, H., NANDI, S.P., and WALKER, P.L. 1972. Nature of the porosity in American coals. *Fuel*, vol. 51. pp. 272–277.
- GEARHART OWEN INDUSTRIES. 1975. Formation evaluation data handbook. Fort Worth. TX.
- GRAY, V.R. 1983. A formula for the mineral matter to ash ratio for low rank coals. *Fuel*, vol. 62. pp. 94–97.
- HUANG, H., WANG, K., BODILY, D.M., and HUCKA, V.J. 1995. Density measurements of Argonne Premium coal samples. *Energy & Fuels*, vol. 9. pp. 20–24.
- KING, J.G. and WILKINS, E.T. 1944. The internal structure of coal. *Proceedings of the Conference on Ultra-fine Structure of Coals and Cokes*, London, 1943. British Coal Utilization Research Association, London. pp. 46–56.
- LAUBACH, S.E., MARRETT, R.A., OLSON, J.E., and SCOTT, A.R. 1998. Characteristics and origins of coal cleat: A review. *International Journal of Coal Geology*, vol. 35. pp. 175–207
- LEVINE, J.R. 1993. Exploring coalbed methane reservoir. Short Course, Institut Francais di Petrole, Rueil-Malmaison. 265 pp.
- MCENANEY, B. and MAYS, T.J. 1989. Porosity in carbons and graphites. *Introduction to Carbon Science*. Marsh, H. (ed.), Butterworths, London. pp. 153–196.
- MCGRAW-HILL. 1984. Dictionary of Scientific and Technical Terms. 3rd edn. New York.
- MEYERS, A., CLARKSON, C., WEX, T., and LEACH, B. 2004. Estimation of *in-situ* density of coal and relative density analyses: *Final Report for ACARP Project C10042*. Australian Coal Association Research Programme, Brisbane.
- MORLEY, C. 2003. Beyond reconciliation – A proactive approach to using mining data. *Proceedings of the Fifth Large Open Pit Conference*, Kalgoorlie, 3–5 November 2003. Australasian Institute of Mining and Metallurgy, Melbourne. pp. 185–191.
- NEBEL, M.L. 1916. Specific gravity studies of Illinois coal. University of Illinois *Bulletin*, vol. XIII, no. 44. Engineering Experiment Station, July 1916. Urbana, IL.
- NOPPÉ, M. 2004. Reconciliation: importance of good sampling and data QA/QC. *Proceedings of the Mining and Resource Geology Symposium*. XYZ, EGRU Contribution no. 62.
- PRESTON, K. 2005. Estimating the *in situ* relative density of coal – Old favourites and new developments. *Proceedings of the Bowen Basin Symposium 2005. The Future for Coal – Fuel for Thought*, Beeston, J.W. (ed.). Geological Society of Australia, Coal Geology Group and the Bowen Basin Geologists Group, Yeppoon, Queensland. pp. 13–22.
- PRESTON, K. and SANDERS, R. 2005. Calculating reserves – A matter of some gravity. A study by Quality Coal Consulting Pty Ltd for Pacific Coal Pty Ltd.
- PRESTON, K.B. and SANDERS, R.H. 1993. Estimating the *in-situ* relative density of coal. *Australian Coal Geology*, vol. 9, May. pp. 22–26.
- REES, O.W. 1966. Chemistry, uses and limitations of coal analyses. *Report of Investigations 220*. Illinois State Geological Survey. 55 pp.
- ROBECK, E. and HUO, D. 2015. Pure coal and mineral matter properties: A practical foundation for *in situ* density estimation. Peabody Energy, St. Louis, MO.
- RODRIGUES, C.F. and LEMOS DE SOUSA, M.J. 2002. The measurement of coal porosity with different gases. *International Journal of Coal Geology*, vol. 48. pp. 245–251.
- ROUX, L. 2012. Optimal yield and cut density prediction of semi soft coking coal and powerstation coal in the Waterberg Coalfield, Limpopo Province. MSc dissertation, University of the Witwatersrand, Johannesburg.
- ROUX, L. 2017. The application of ash adjusted density in the evaluation of coal deposits. PhD thesis, University of the Witwatersrand, Johannesburg.
- SMITH G.G. 1991. Theoretical estimation of *in-situ* bulk density of coal. *CIM Bulletin*, vol. 84, no. 949. pp. 49–52.
- UNSWORTH, J.F., FOWLER, C.S., and JONES, L.F. 1989. Moisture in coal: 2. Maceral effects on pore structure. *Fuel*, vol. 69. pp. 18–26.
- VAN KREVELEN, D.W. 1993. Coal: Typology–Physics–Chemistry–Constitution. 3rd edn. Elsevier, Amsterdam. 979 pp.
- WANG, X. 2007. Influence of coal quality factors on seam permeability associated with coal bed methane production. PhD thesis, Faculty of Science, University of New South Wales.
- WARD, C.R. (ed.). 1984. Coal Geology and Coal Technology. Blackwell Scientific, Melbourne. 345 pp.
- WARD C.R. 2002. Analysis and significance of mineral matter in coal seams. *International Journal of Coal Geology*, vol. 46. pp. 67–82.
- WEBB, P.A. 2001. Volume and density determinations for particle technologists. Micromeritics Instrument Corp., Norcross, GA. ◆