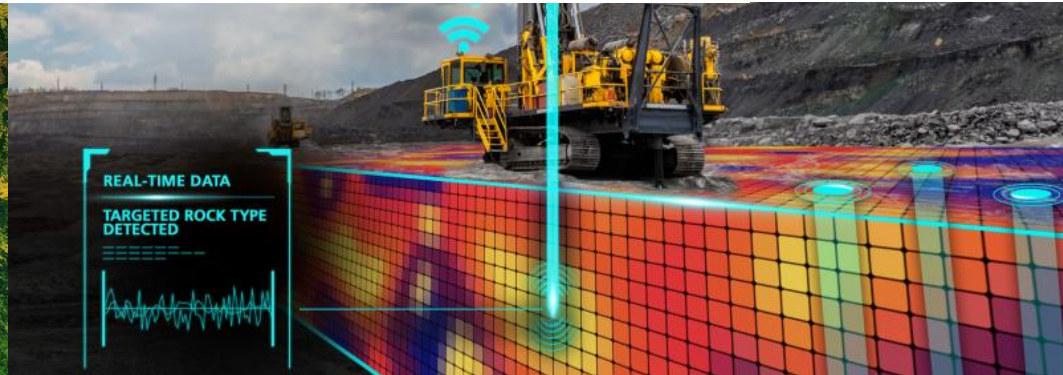
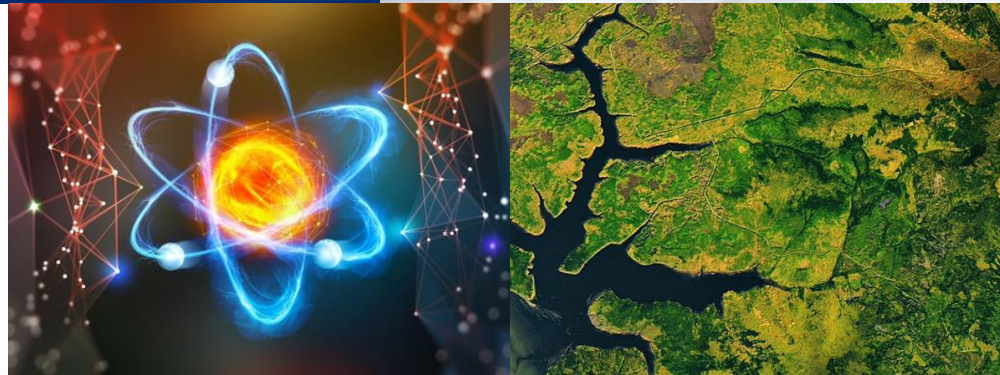
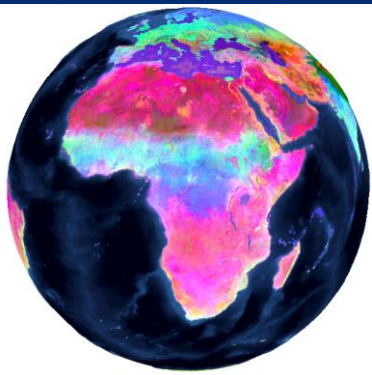




Are Variational Gaussian Processes the Missing Link in Predictive Geometallurgy?

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Compartments limit adoption of Geomet

- Mining doesn't run on a value chain; it runs on islands (i.e., compartments/segmented disciplines).
- Every arrow here is a hand-off where uncertainty dies and a spreadsheet is born.
- We export a number; the next team imports a fact.
- Today I'll show a way to keep uncertainty alive across the chain.





Toward Coherent Predictive Geometallurgy



Statistics

“Discipline that concerns the collection, organisation, analysis, **interpretation**, and presentation of **data**.”

Geostatistics

“Branch of statistics **focusing on spatial** or spatiotemporal datasets.”



Machine learning

“Field of study in artificial intelligence concerned with the development and study of statistical algorithms that can **learn from** and generalise to unseen **data** and thus perform tasks **without explicit instructions**.”

We need a name to unify the new discipline!

- Geo-machine intelligence?
- Spatio-temporal big data analytics?
- Geostatistical learning?
- Geodata Intelligence?



Fog of War

- Your model is a **scout**, not an **oracle**!
- The question isn't *what* it reveals, it's *how far that revelation is reliable*.
- **Spatial awareness:** We need to know how far we can trust it.



Source: <https://medium.com/@travnick/fog-of-war-282c8335a355>

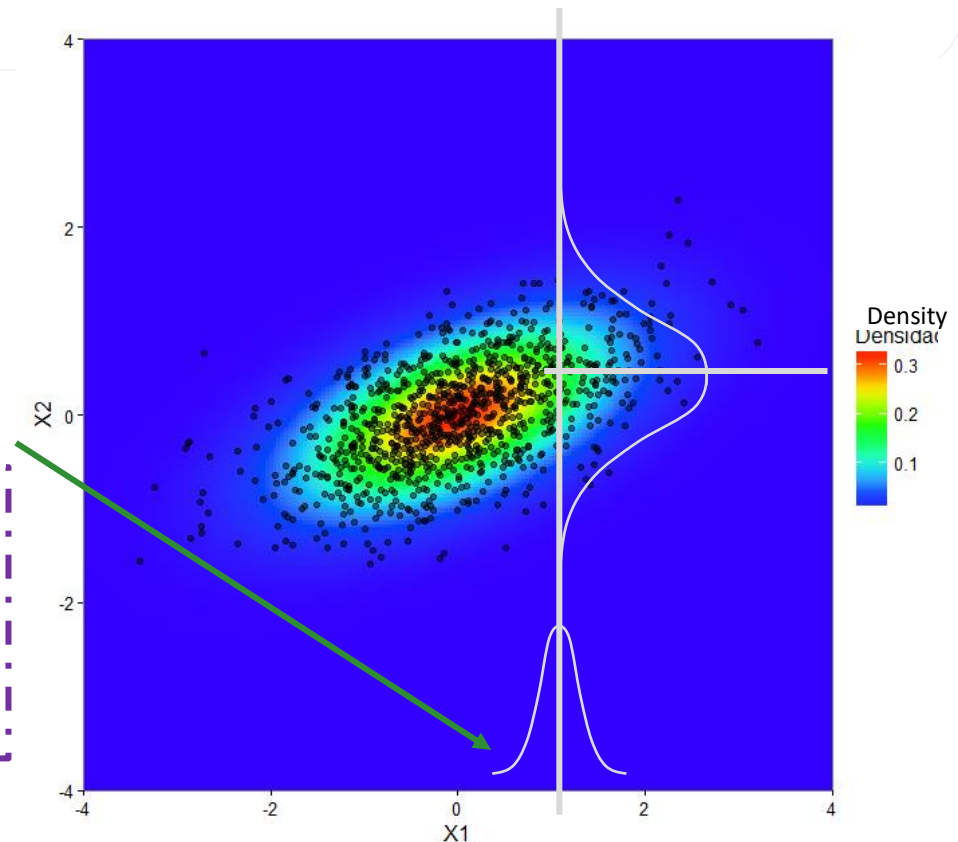
Variational Gaussian Processes (VGP): Calibrated Uncertainty at Deposit Scale

Given a noisy observation of x_1 , we update our belief about x_2 : the mean shifts towards what x_1 suggests, and the variance shrinks; both by amounts determined by correlation and noise.

$$p(x_2|x_1) = \mathcal{N}\left(\underbrace{\frac{\sigma_1\sigma_2\rho_{12}}{\sigma_1^2 + \Lambda}}_{\text{Conditional Mean}} (x_1 - \mu_1) + \mu_2, \sigma_2^2 \underbrace{\left(1 - \frac{\sigma_1^2\rho_{12}^2}{\sigma_1^2 + \Lambda}\right)}_{\text{Conditional Uncertainty}}\right)$$

- If **one value is known**, it can be used to obtain **the conditional distribution** for the other.
- If one value is only **approximately known**, it is still able to provide some information.

Gonçalves, Í. G., & Wellmann, F. (2025).



Case study: Assen Fe Deposit (South Africa)



Reality in BIF deposits

- Heterogeneous chemistry/texture/density across domains.
- Blend stability, energy use, and spec risk vary spatially.



Why classical GP/co-kriging fall short

- With 30,000 samples and 5 outputs, **standard GP and co-kriging is about 10^{13} FLOPs**, while a **variational GP lands near 10^{10}** . That's roughly a **1000-fold** saving versus exact GP.



Testable question

- Can a scalable, compositionally coherent VGP support rock classification, multi-element prediction, density estimate and energy decisions?

How the VGP geometallogy pipeline works



Input Data

X
Y
X
Rock type
Mineralogy
Texture
Density
Al₂O₃
CaO
FeO*
K₂O
MnO
P₂O₅
SiO₂
TiO₂
BWI

Data Transformation

Centered log ratio (CLR) transformation
↓
PCA
↓
3D Anisotropy

Inducing Points
⋮
Grid 3D
⋮
K-means++

GP-Walk
Coordinate-warping layer

GP (Geol) Matérn32

GP (Geol) Linear

Concatenate

GP (Comp) Spherical

Concatenate

GP (Density) Spherical

Concatenate All

XYZ

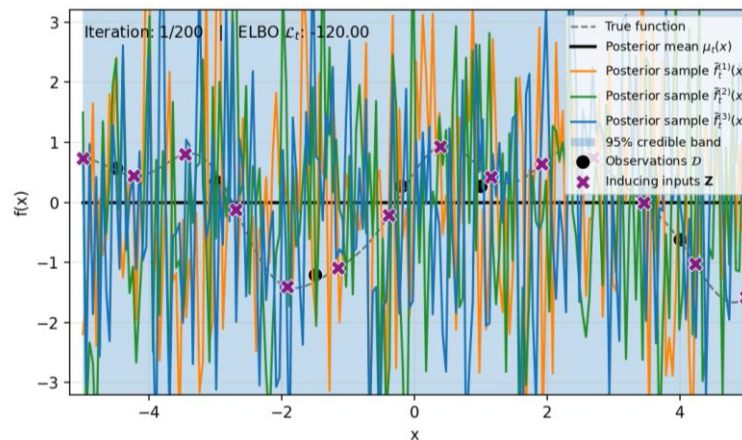
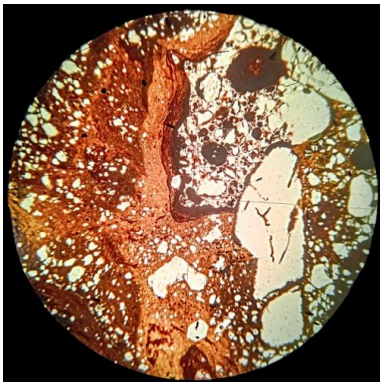
Geology ± Δ

Compositional data ± Δ

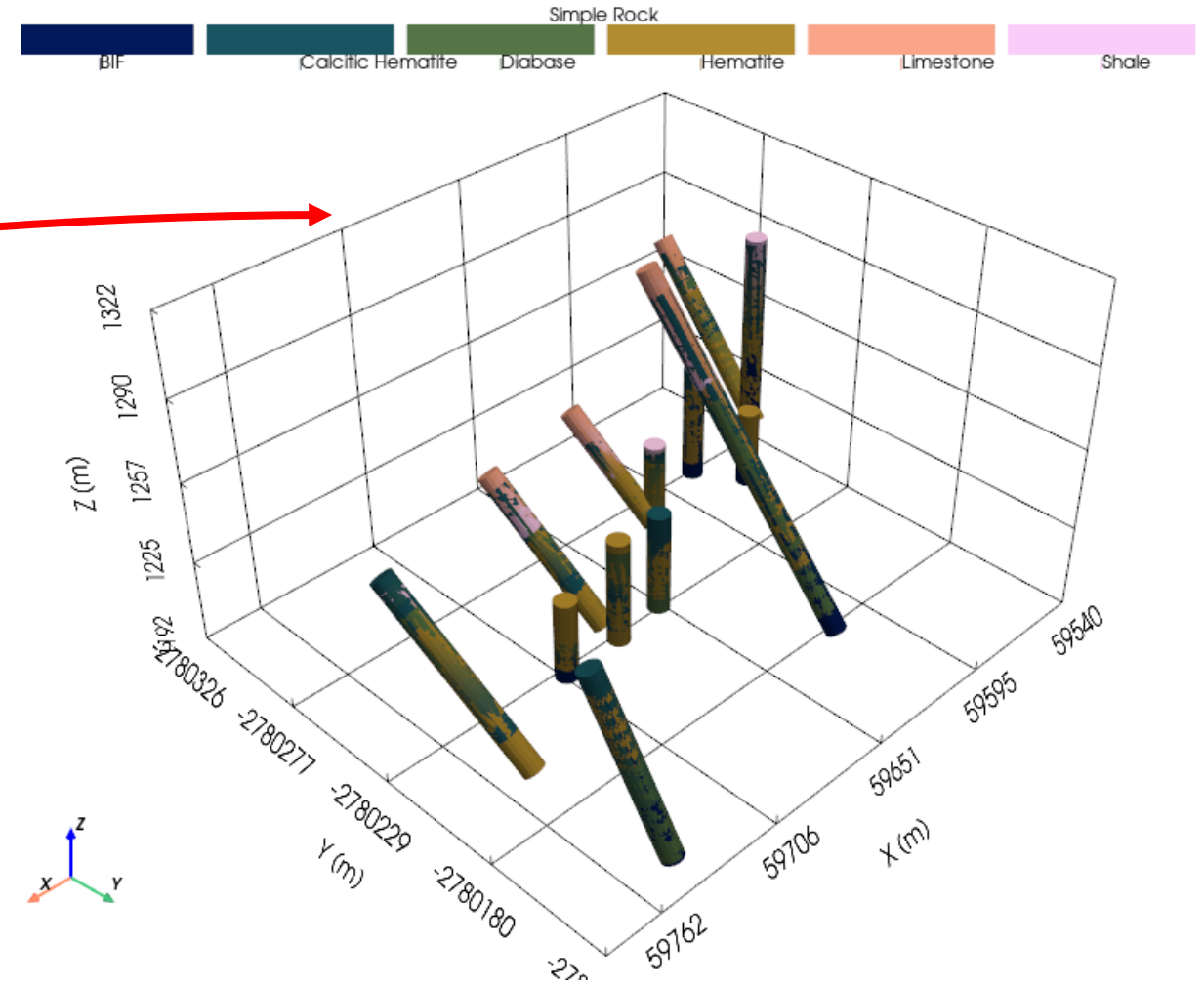
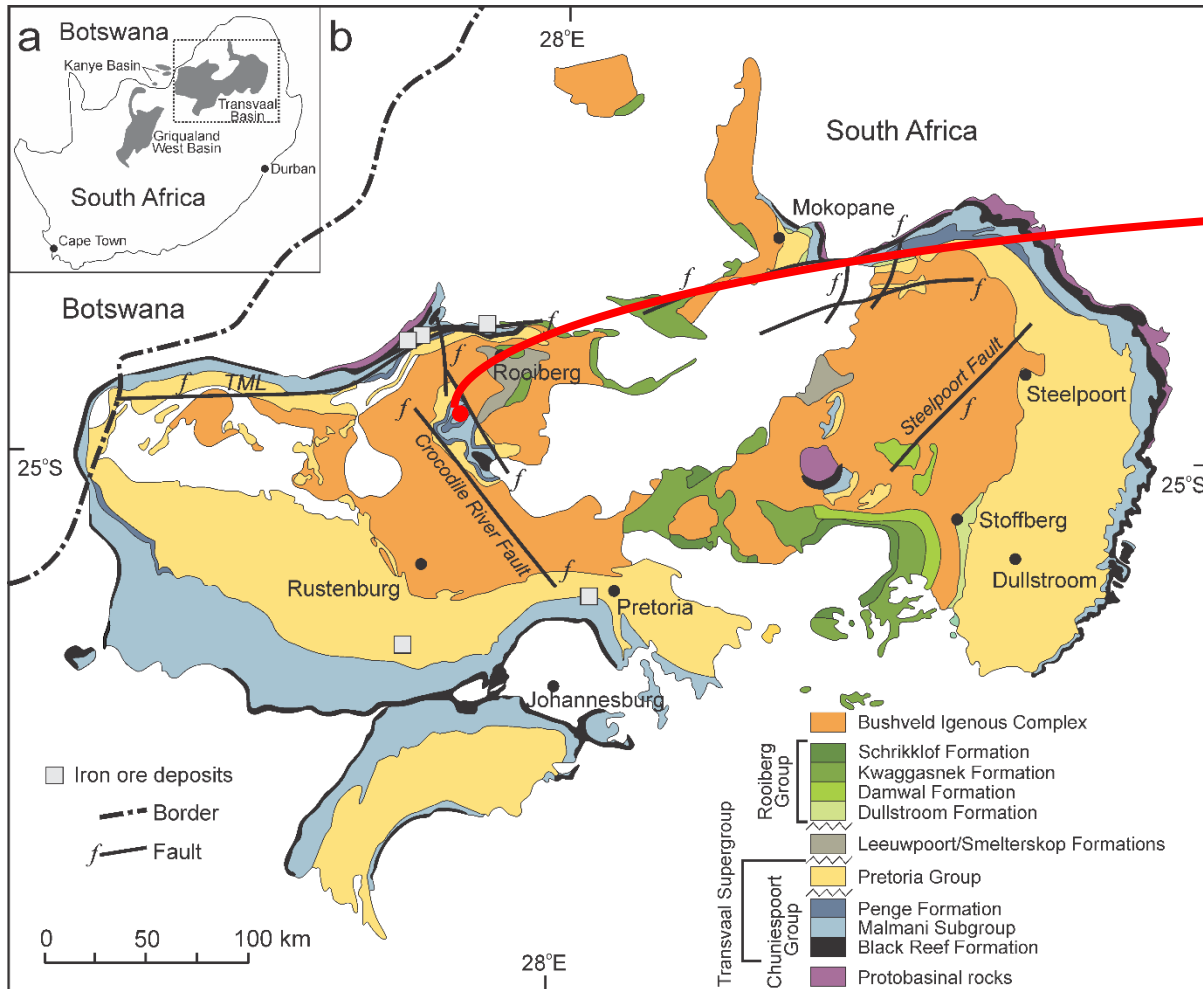
Density ± Δ

=

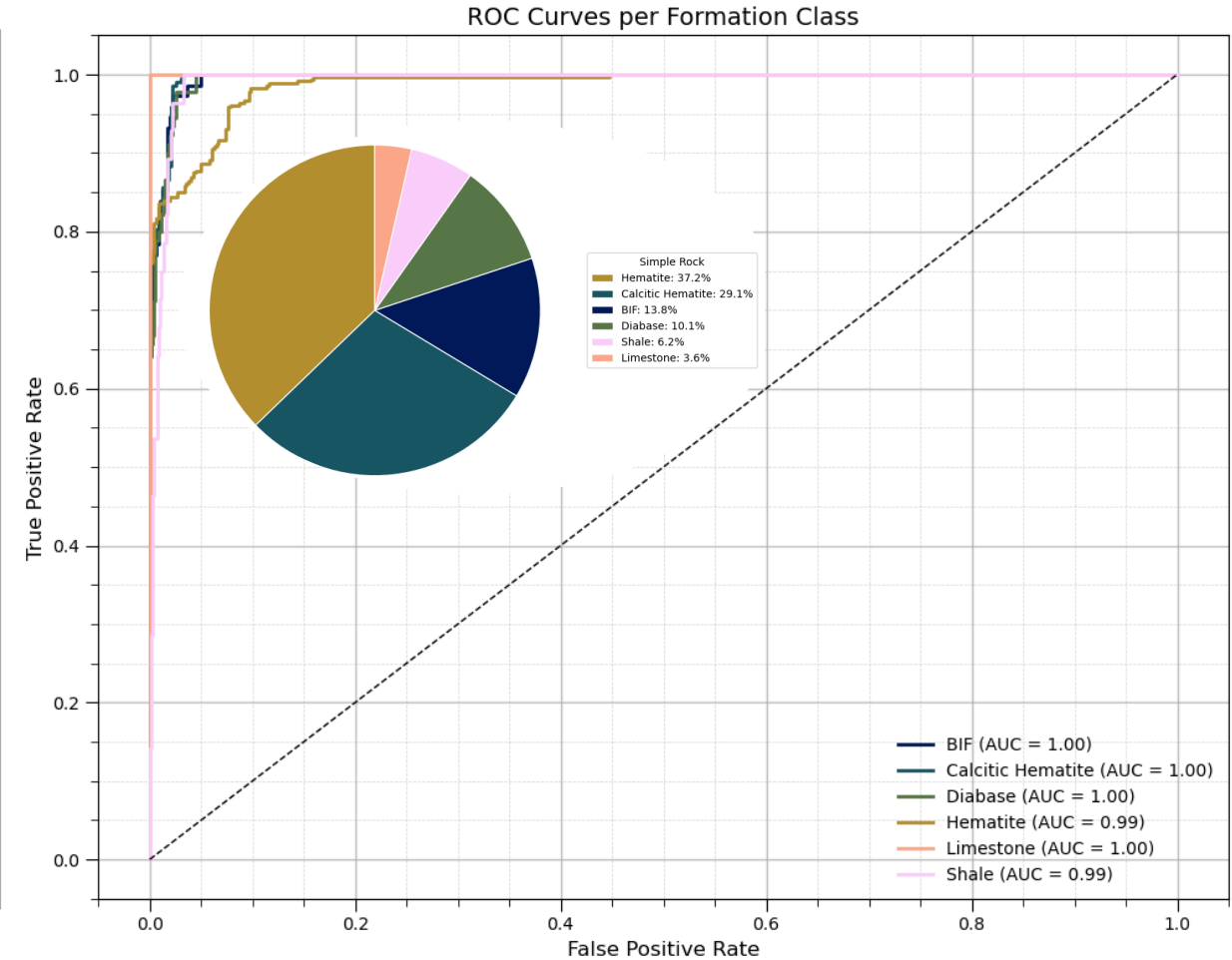
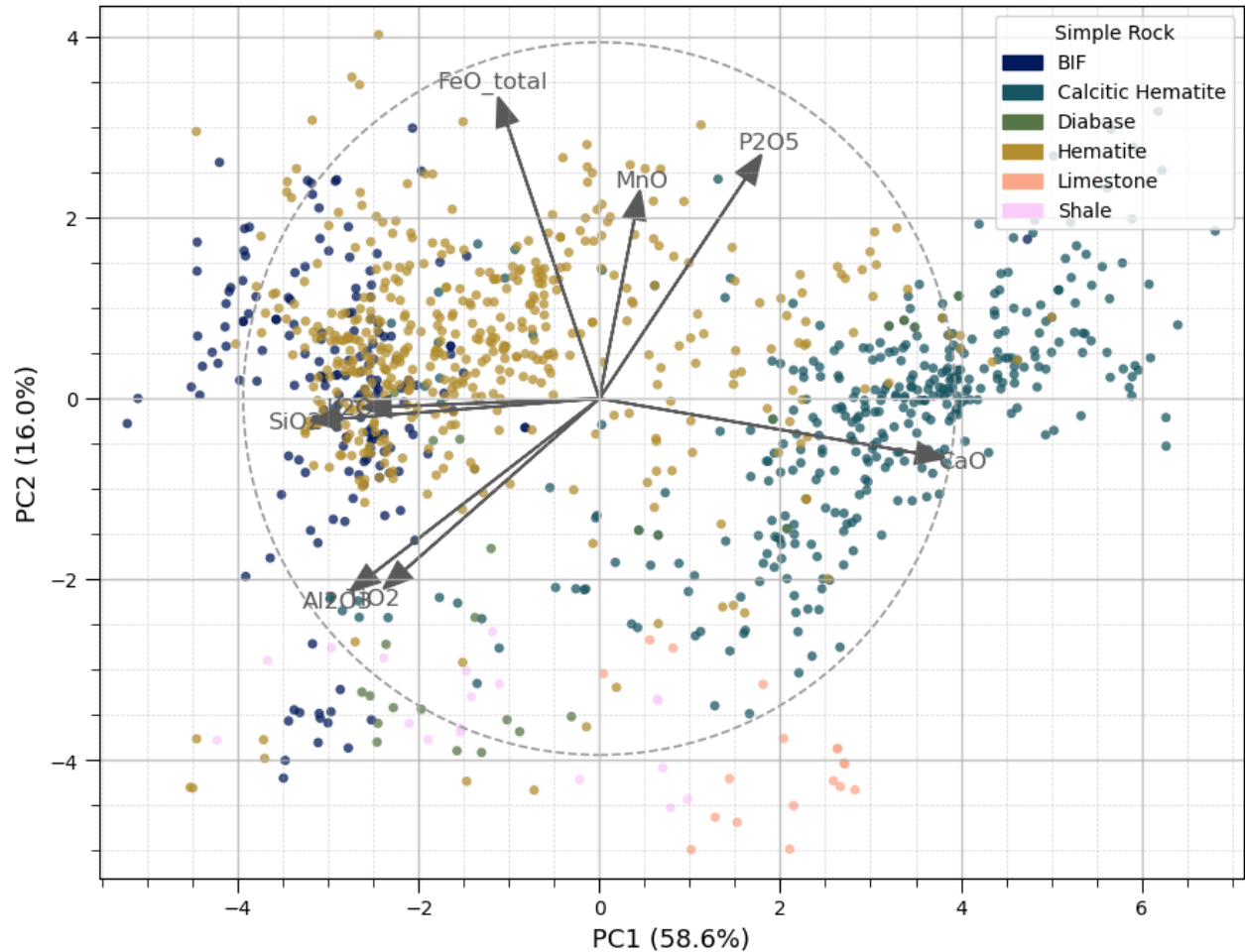
BWI ± Δ



Implicit Geological Modelling

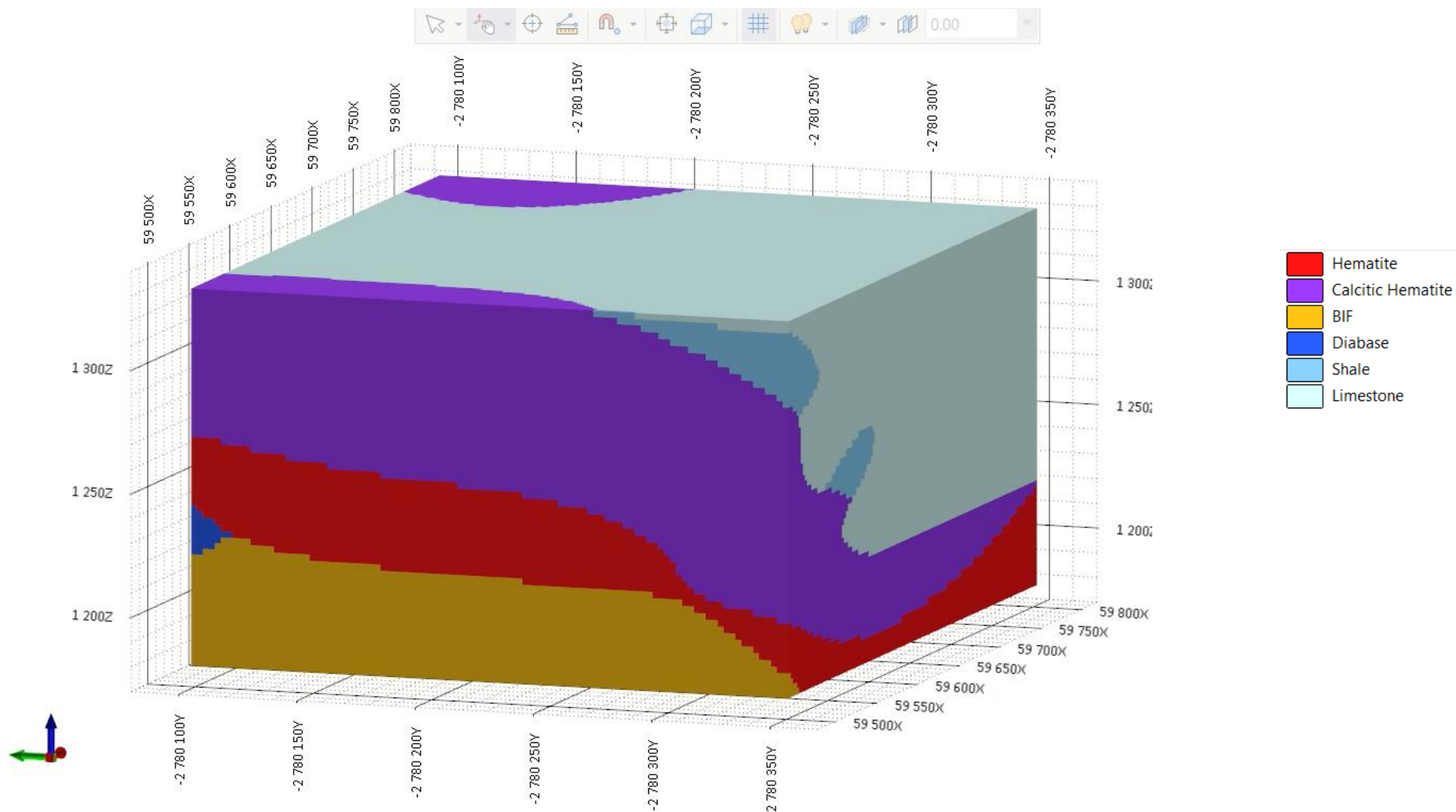


Implicit Geological Modelling



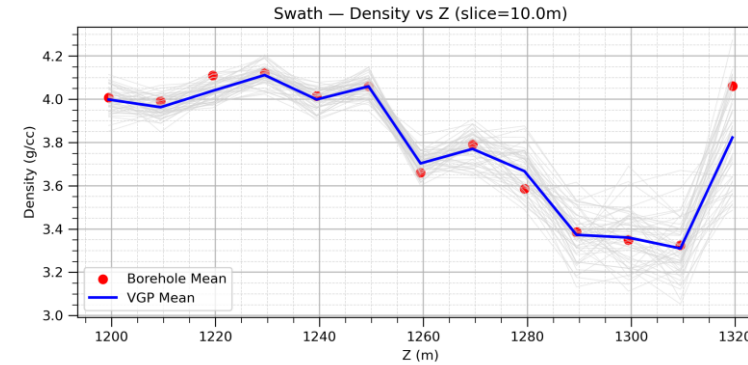
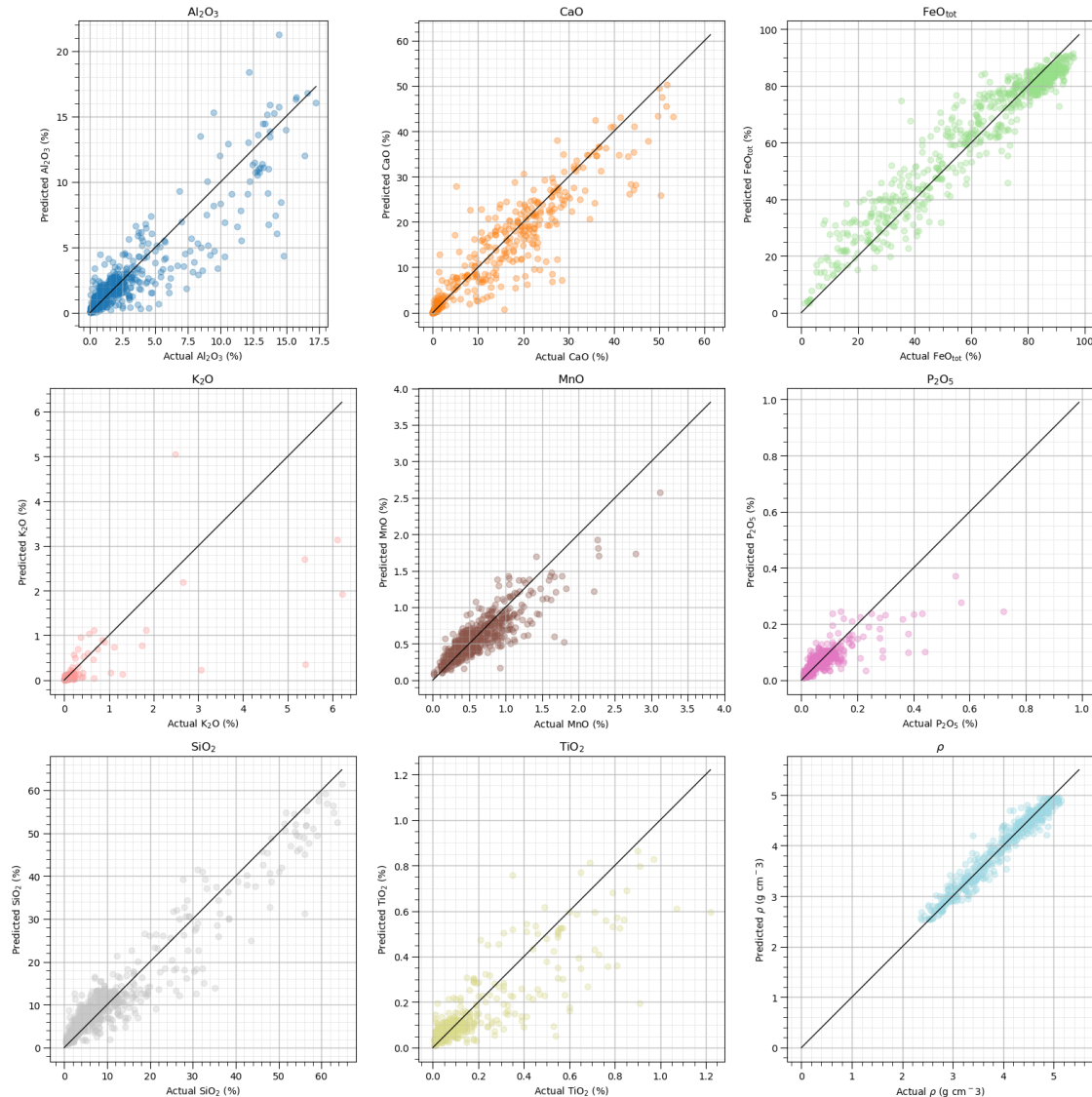


Implicit Geological Modelling

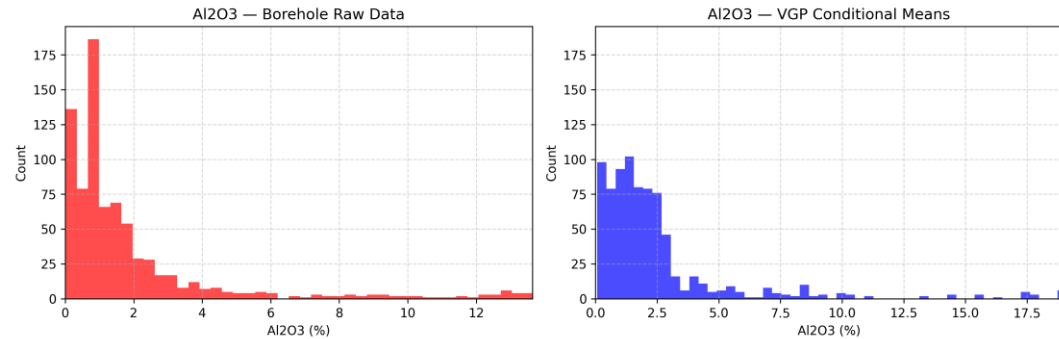


Setting calibrated business rules

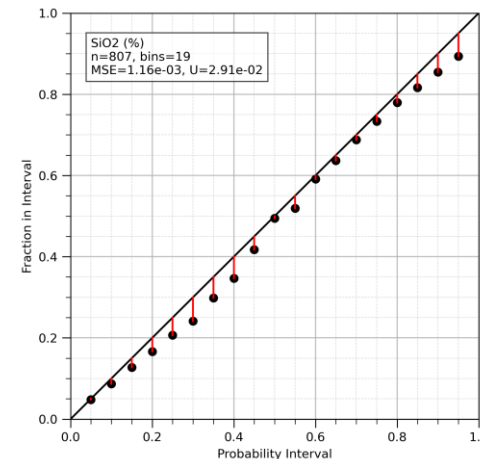
Actual Versus VGP Prediction



Swath Plots



PDFs

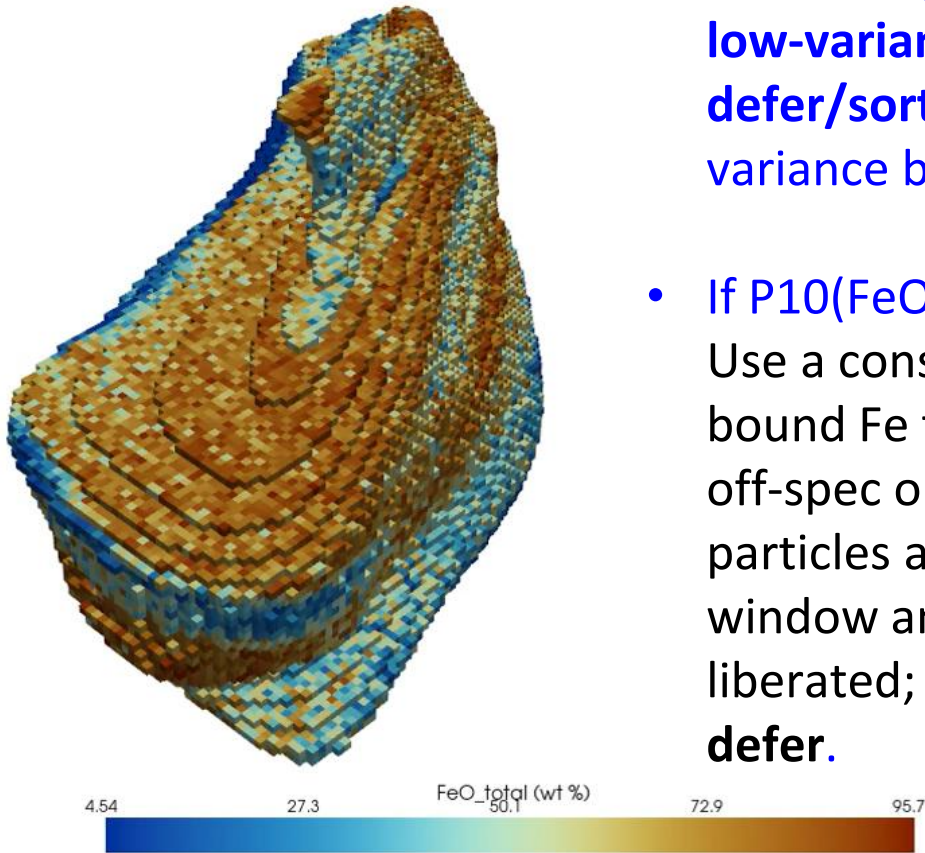


- **X-axis (probability/coverage asked for):** target/nominal coverage of your predictive interval (e.g., 0.7 $\Rightarrow$ “70% should contain the truth”).
- **Y-axis (probability/coverage achieved):** empirical fraction of cases where the truth actually fell inside those intervals for each bin.
- **45° Line:** on line = calibrated; below = under-coverage/over-confident; above = over-coverage/conservative.

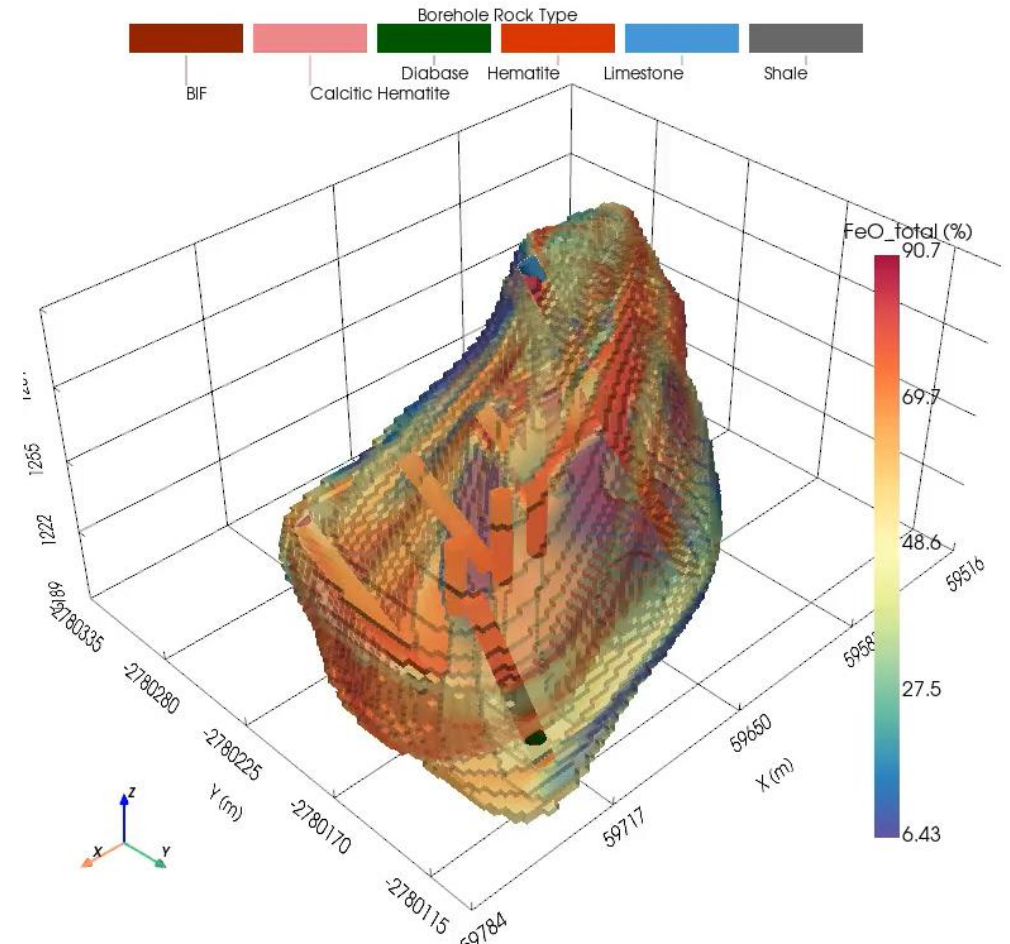
FeO_{total} Uncertainty Quantification

Multiple VGP Realisations

- **Scheduling:** advance **high-Fe, low-variance** blocks; **defer/sort** low-Fe or high-variance blocks.
- If $P10(\text{FeO}_{\text{total}}) \geq \text{Fe min} \rightarrow$ Use a conservative lower-bound Fe to schedule; send off-spec ore to **jig/DMS** when particles are in the right size window and sufficiently liberated; if not, **stockpile or defer**.

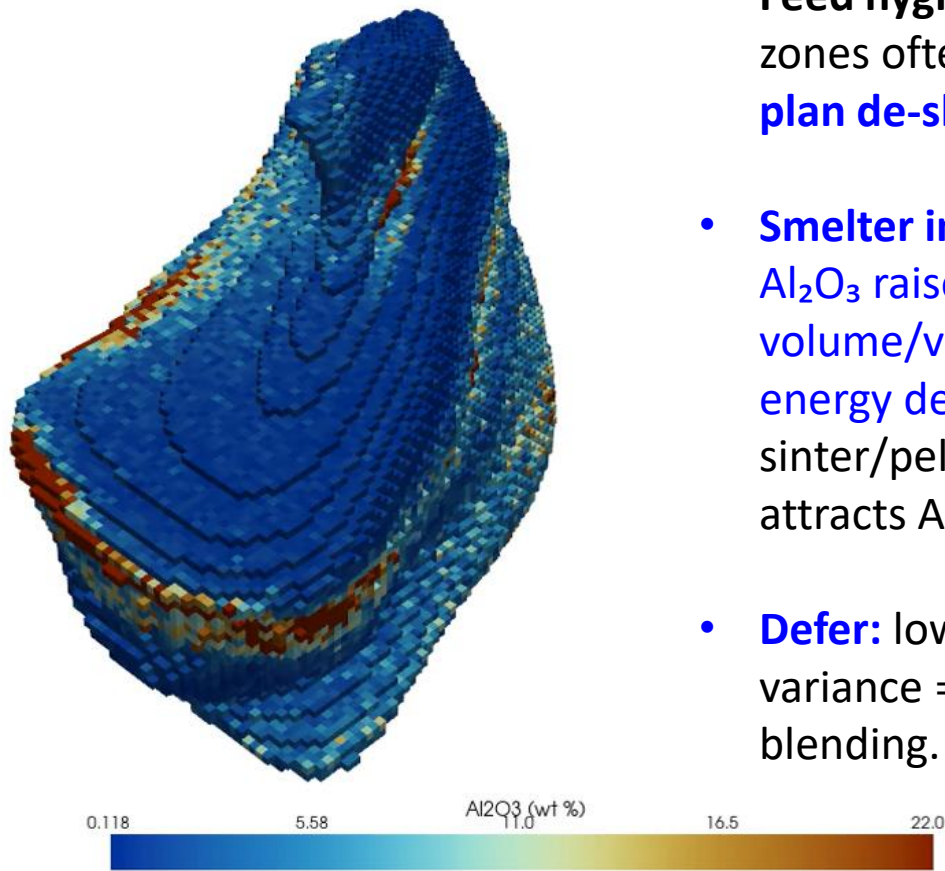


VGP Final Model



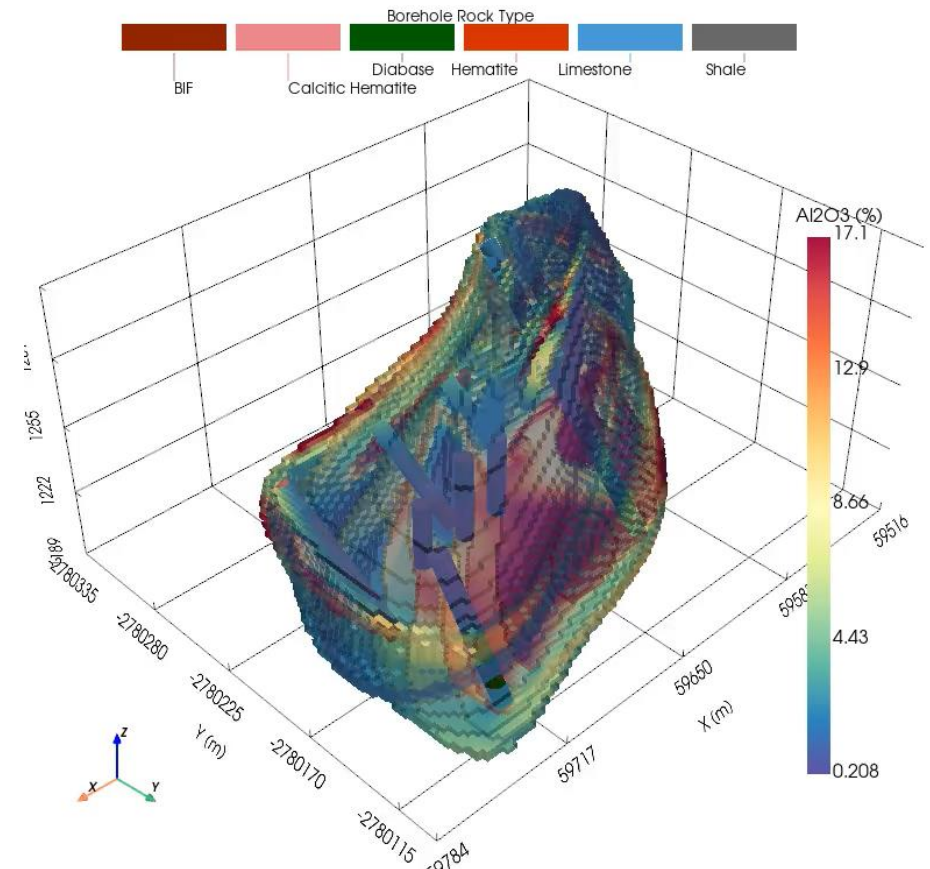
Al₂O₃ Uncertainty Quantification

Multiple VGP Realisations



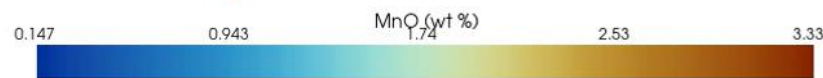
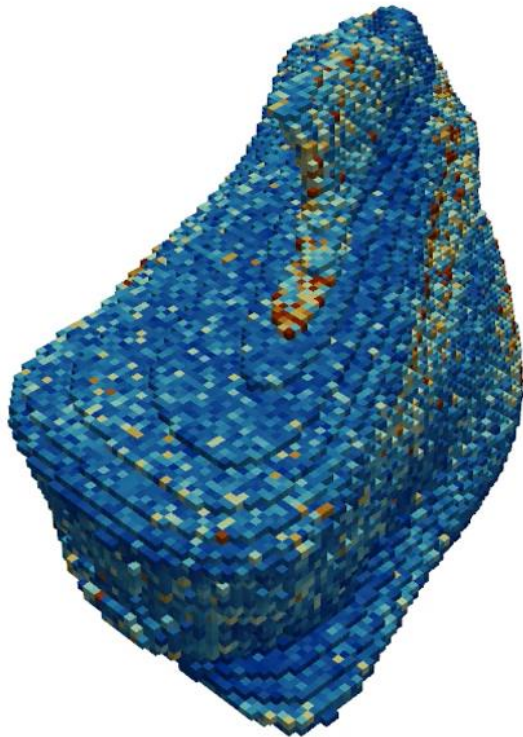
- **Feed hygiene:** high-variance zones often = **clays/kaolinite**; **plan de-sliming at source.**
- **Smelter implication:** High Al₂O₃ raises slag volume/viscosity, lifts flux and energy demand, affect sinter/pellet quality, and attracts Al₂O₃ penalties.
- **Defer:** low Fe + high Al₂O₃ variance ⇒ park or drill before blending.

VGP Final Model



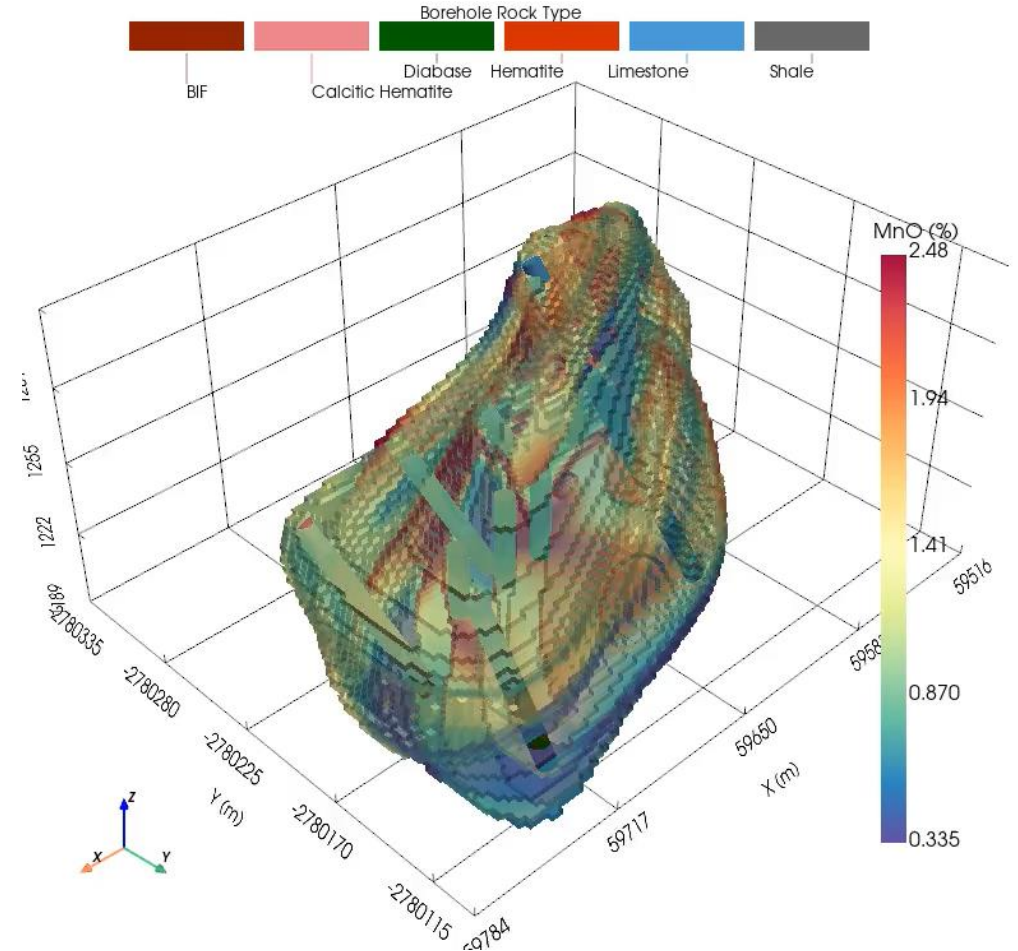
MnO Uncertainty Quantification

Multiple VGP Realisations



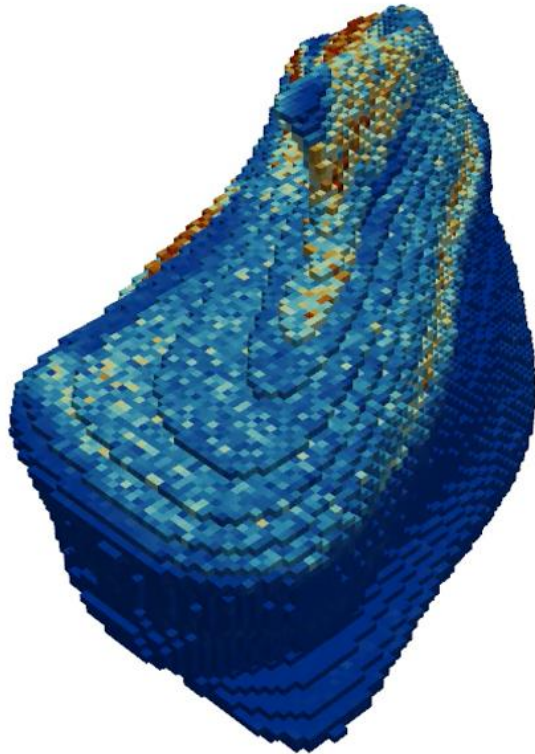
- Map streaks of high MnO for segregation or ore sorting (density/optical/X-ray).
- **Smelter/steelmaking:** High MnO raises flux demand and slag viscosity, increases energy/coke, affects hot-metal quality; **contract penalties** apply once MnO (or Mn/Fe) exceeds product limits.
- **Upgrade with controls:** Moderate MnO but stable $\Rightarrow$ magnetics + classification; tune **basicity (CaO)** to keep slag manageable.

VGP Final Model



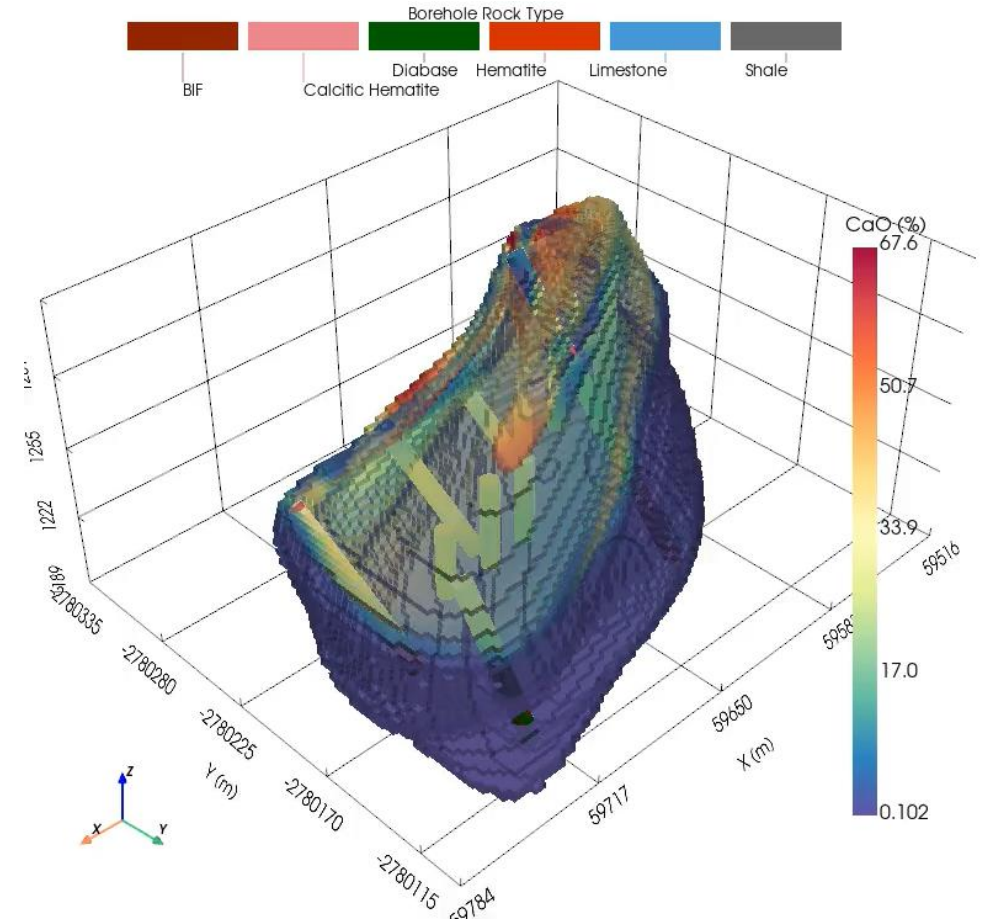
CaO Uncertainty Quantification

Multiple VGP Realisations



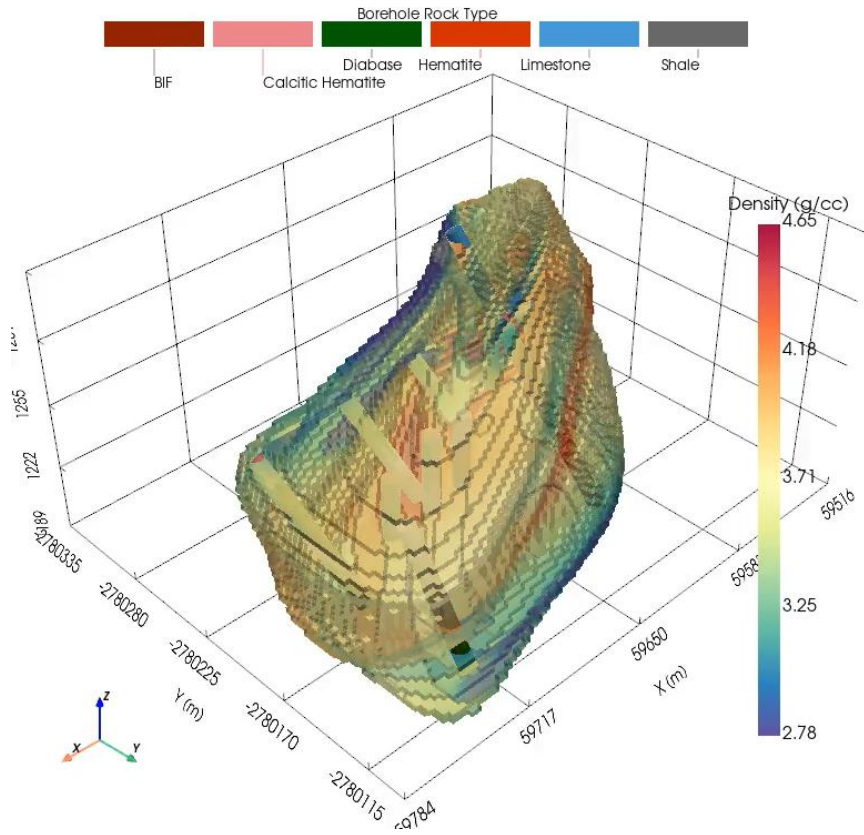
- Early mass rejection via density/optical/X-ray sorting.
- Dedicated low-temperature calcination when economic.

VGP Final Model



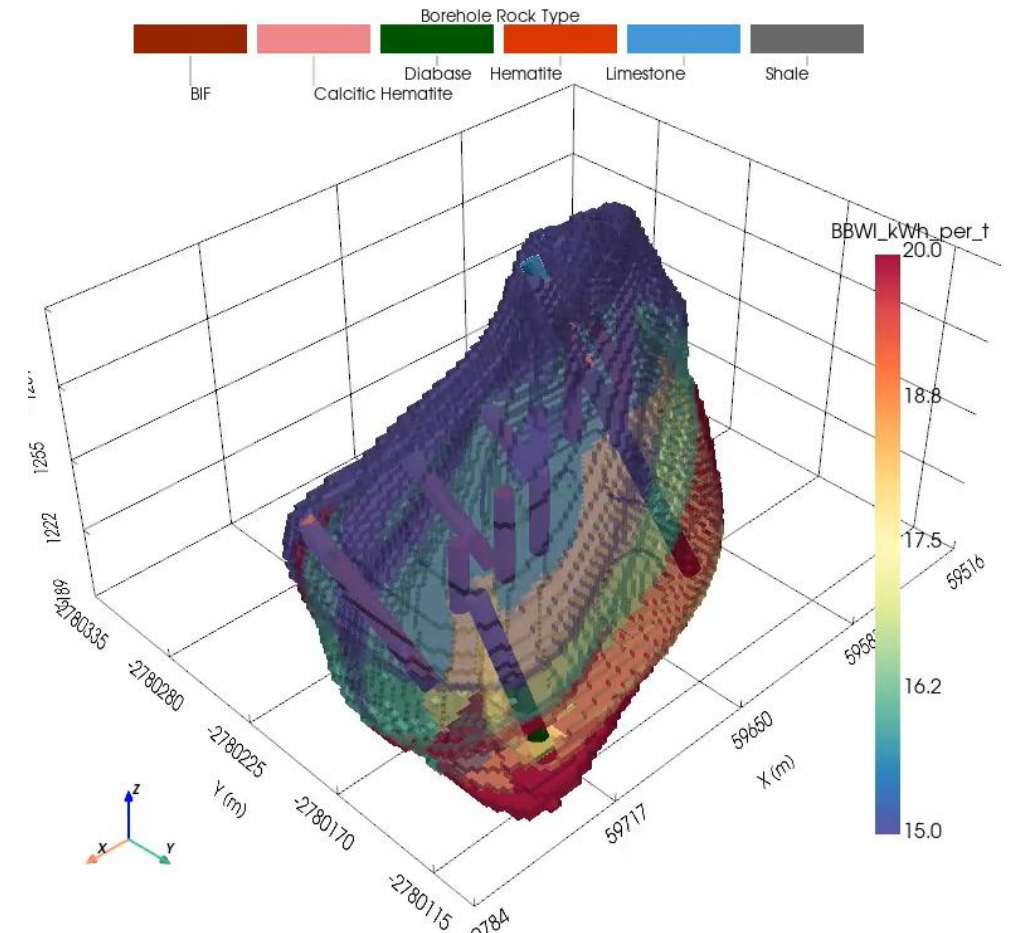
Density and BWI

Specific Gravity (t/m³)



- Higher SG tracks hematite; lower SG marks siliceous/carbonate/clay zones.
- High BWI correlates with **silica-rich BIF**; lower BWI aligns with **massive hematite**.
- Route guardrails:** Require $\text{Fe P10} \geq \text{Fe min}$, $\text{SiO}_2 \text{ P90} \leq \text{cap}$, $\text{Al}_2\text{O}_3 \text{ P90} \leq \text{cap}$, $\text{BWI P90} \leq \text{energy cap}$ for premium blend; otherwise **upgrade (sort/float)** or **defer**.

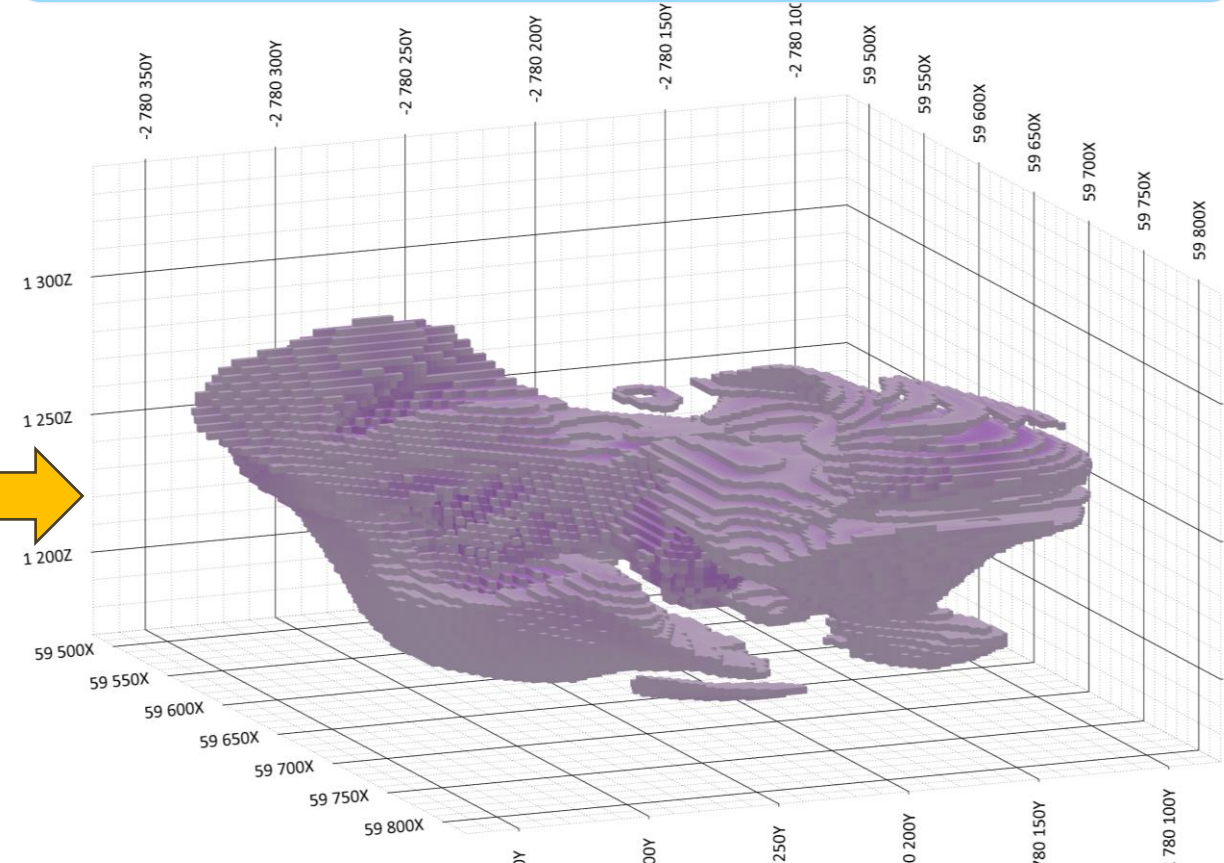
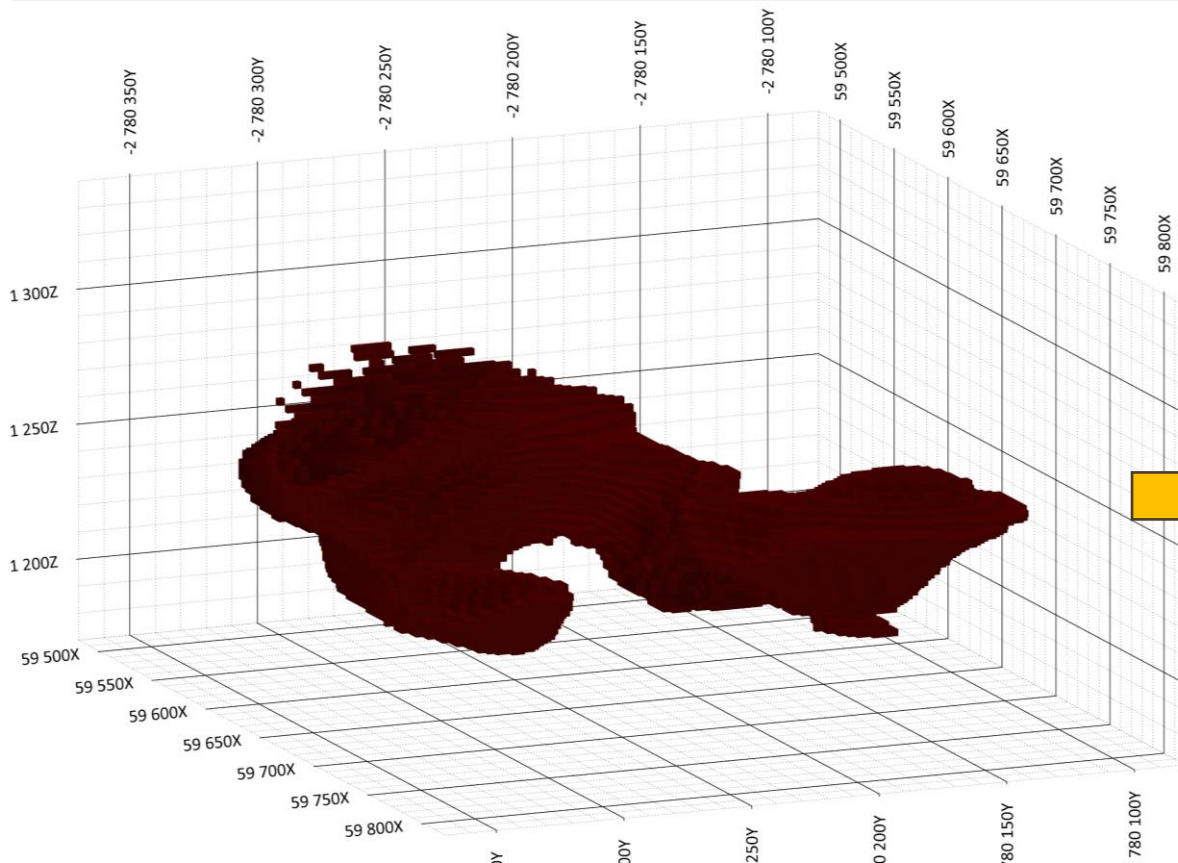
Bond Work Index (kWh/t)



Value proposition: Minimise uncertainty upstream; reduce cost downstream

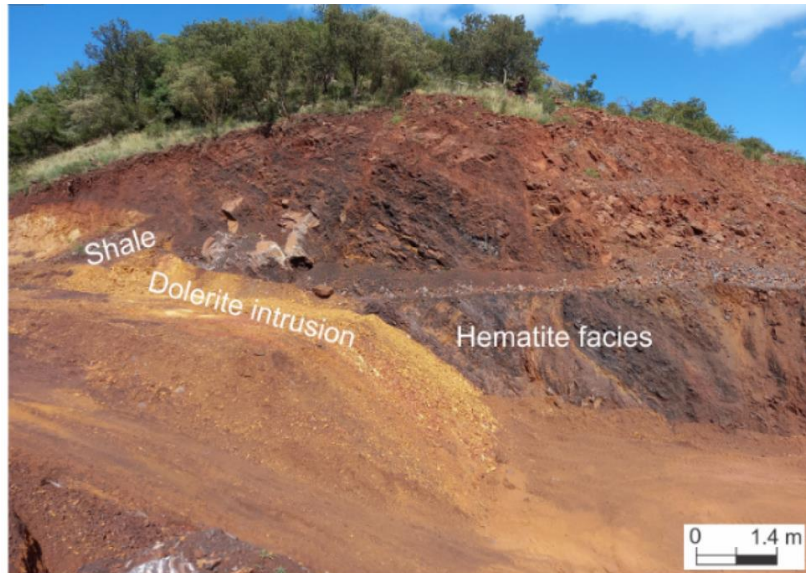
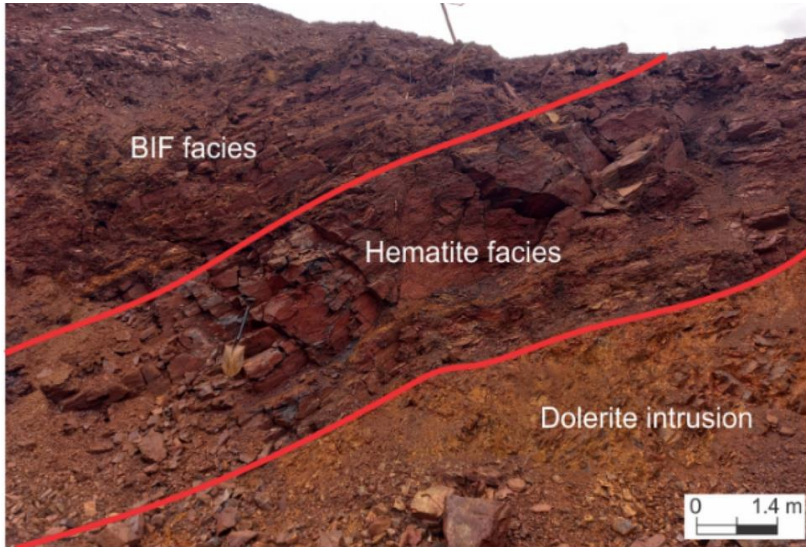
Filter Mineral Reserves for Mine Planning

Design the Mine based on Geomet Model



Turn compliant tonnes into executable tonnes: filter by geomet constraints, then design to the ore's behaviour.

Key Takeaways



1. Variational Gaussian Processes give calibrated ranges, not just single numbers, so blending, routing, and drilling are set to a risk matrix, *not hope*.



2. Multi-element/oxides are modelled coherently with geology making downstream *slag, blend, and spec checks trustworthy*.



3. Simple rules on Fe, Al_2O_3 , MnO, density, and BWI turn maps into actions: tighten or relax envelopes, route to jig/DMS when size–liberation allow, sort early, or defer..



4. Fewer surprises: Using conservative percentiles for grade and energy cuts penalties, sizes equipment sensibly, reduces blend volatility, and focuses drilling where it most lowers risk.





Thank You



micromine
origin & beyond